Researches on the Application of the New improved Analytic Hierarchy Process in the Physical Achievements Inspection System

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Abstract

The physical class is always out of the door. This class model is different from the traditional class. As this special characteristic, how to ensure the weight of the sports test course achievement evaluation becomes necessary and important. The application of AHP makes it possible to carry out the quantity evaluation in the sports research. The study makes a comprehensive evaluation with AHP and puts forward a method for relative analysis and a thereunder for decision-maker. From the necessary and sufficient conditions of completely consistent matrix, the criterion of consistency has been improved. We create a new improved AHP method, namely MCAHP (matrix correction analytic hierarchy process). And we apply it to examine the physical class in determining the weights of evaluation indicators by students. Examples show that the improved algorithm is better than the original AHP in significantly reduced computation. And this method improves the running speed. The first part is the introduction. The second part is the steps of AHP. The third part is the study on the MCAHP algorithm. The fourth part is the last part is the conclusion.

Keywords: MCAHP, Physical Achievements Inspection System, Analysis

1. Introduction

Compared with the traditional culture education, the physical education attends the classes outside in most cases. In addition, the number of inspections is less than the traditional culture education. Due to the particularity of the physical education, it becomes a key factor to judge the weights of the student physical test course achievement evaluation indexes.

Yan Linlin, Zhang Wenge and Wu Jingqi analyzed the physical factors of college physical education evaluation system [1]. They used the method of literature and investigation to study the comprehensive evaluation system in colleges and universities at present. They also focused on the analysis of the current situation of the physical indexes which relate to the health status of university students. In addition, they put forward to make full use of the guiding and excitation function to solve the increasingly serious health problems and achieve the comprehensive development for students. Peng Shuolong studied the indicators which affected the sports development factors [2]. He studied and analyzed the most direct and the most significant factors which effected the development of the competitive sports from different levels and different angles. Adopting the method of the stepwise regression to list the optimal equation, he carried on the quantitative analysis of the optimal index which effected the development of competitive sports from the macroscopic, meso and microcosmic levels. Aiming at enriching the sport theory of the qualitative research and providing the scientific basis for formulating policies on sports, Liu Houlin and Bu Deshou explored a new formula of the mean test on the physical statistics [3]. They pointed out that the mean test of the current physical indexes is two different types. And they proposed a new mean test statistic function for the first time according to the type of the probability characteristics.

The investigation of the physical examination course achievement evaluation index is a complex system with multi-factors. However, some problems cannot be established as the mathematical model for the quantitative analysis. Due to the tight time, some problems may not be quantitatively analyzed. We just need to make a preliminary selection and a general assessment. The decision makers face a choice, and it is difficult to make an objective evaluation. This paper attempts to apply the analytic hierarchy process to conduct the comprehensive assessment of the physical examination course achievement evaluation index. Further, this paper seeks a simple and objective evaluation method.

Because of the disadvantages of the traditional AHP method, many scholars put forward an improved AHP method. Some scholars put forward the fuzzy AHP method [4-7]. The method combines the analytic hierarchy process with the fuzzy comprehensive evaluation. This method uses the AHP method to determine the weight of each index in the evaluation system. In addition, it uses the fuzzy comprehensive evaluation method to evaluate the fuzzy indexes. The AHP fuzzy method solves the fuzzy problems perfectly. Later, some scholars proposed an AHP-Entropy method [8-10]. The entropy method is the objective weighting method, and it determines the attribute weights according to the contact degree of each attribute or the size of the information which is provided by each attribute. The AHP-Entropy portfolio analysis method considers the index data and the subjective preference of the index for the decision makers. With the proposed of the grey theory, scholars combine the AHP method with the grey theory and put forward a Grey-AHP method [11-13]. This method disposes the decentralized information of the evaluation experts to a weight vector which describes the different grey degrees. On the basis, we make the single value processing. Then, we can get the comprehensive evaluation value of the evaluation system. Because this method combines the grey theory, it can be mainly used to handle the uncertain systems of small sample and poor information.

Constructing the judgment matrix which meets the consistency requirement is one of the key issues of AHP. We intend to improve the consistency of the possibility of the judgment matrix and performance of AHP. We revise judgment matrix which does not meet the consistency to improve the possibility of the original matrix consistency on the basis of maintenance the raw data. Thereby, we propose MCAHP (matrix correction analytic hierarchy process) method. And we apply this method to the assessment of the physical examination course achievement index. The experimental results show that the MCAHP algorithm can provide a scientific index system and weights for evaluating the examination courses quickly.

2. The Steps of AHP

Analytic Hierarchy Process is a method for system analysis. This method is proposed by A.L.Saaty at University of Pittsburgh in 20st century. AHP is a simple, flexible and practical multi criteria decision algorithm. This method carries out quantitative analysis for qualitative problems. Index ranking and the weights determination are accomplished by establishing the hierarchical structure model, constructing judgment matrix for each layer, level sequencing and consistency inspection. This method is suitable for multi object decision. It evaluates the degree of each scheme for multiple impact indexes. When a decision is affected by many factors and these are obvious categories among factors, we can choose AHP. We can also use AHP when each index makes quantitative calculation for the influence on the final evaluation without enough data. The characteristic of this method is that can divide the factors in complex problems into interactional levels and make them organized. The method combines judging expert opinion with the objective judgment directly and effectively. Then, this method quantitatively describes the significance of the compared results among factors. At last, we calculate the weights that reflect the orders of importance for factors in each layer.

2.1. Establishing the Hierarchical Structure Model

If we make system analysis, we need group all the factors firstly. Each group is a layer. There are three layers. The destination Layer is the purpose of solving the problem. The criterion layer is to achieve the intermediate links that the targets refer. The project layer is the measures or policies to solve the problems. The hierarchy structure model is shown as Figure 1.



Figure 1. The Hierarchy Structure Model

(1) Constructing the hierarchical structure model and establishing the criterion layer and the index layer

(2) Structural comparison matrix

$$\mathbf{A} = (a_{ij})_{n \times n} \qquad (i = 1, 2, \cdots, n), a_{ij} = 1, a_{ij} = 1/a_{ji}$$

A is the judgment matrix. We set a_{ij} which shows the relative comparison value of a_i index and a_j index.

	<i>a</i> ₁	a 2	 <i>a</i> _{<i>i</i>}
a_1	<i>a</i> ₁₁	<i>a</i> ₁₂	 <i>a</i> _{1 <i>j</i>}
<i>a</i> ₂	<i>a</i> ₂₁	<i>a</i> ₂₂	 a _{2 j}
a _j	<i>a</i> _{j1}	a _{j2}	 a _{ij}

Table 1. The Judgment Matrix

Among them, $a_{ij} > 0, \frac{1}{a_{ij}} = a_{ji}, a_{ii} = 1$. $a_{ji} = 1$

The ratio of Saaty scaling assignment is shown in table 2.

a _{ij}	Index important degree
1	a_i is same important as a_j
3	a_i is a little more important than a_j
5	a_i is more important than a_j
7	a_i is a highly more important than a_j
8	a_i is a extremely more important than a_i
2,4,6,8	The importance between a_i and a_j among the above

Table 2. Scale Meaning of Importance Degree

(3) Judgment matrix A is normalized:

$$a_{ij} = a_{ij} / \sum_{k=1}^{n} a_{kj}$$
 $(i = 1, 2, \dots, n)$

(4) Sum the row of judgment matrix A:

$$\omega_i = \sum_{j=1}^n a_{ij}$$
 (*i* = 1, 2, ..., *n*)

(5) ω_i is normalized:

$$\omega_i = \omega_i / \sum_{i=1}^n \omega_i$$
 $(i = 1, 2, \dots, n)$

(6) To derive the maximum eigenvalue and its eigenvector according to

$$A\omega = \lambda_{\max}\omega .$$

(7) Consistency check We define

$$CI = \frac{\lambda_{\max} - n}{n - 1}$$

C1 is the index of consistency.

When the Judgment matrix has the character of consistency, CI = 0

If $\lambda_{max} - n$ is large, *C1* is large. And the consistency is worse.

For checking whether the judgment matrix has the character of consistency, we compare CI with the index of consistency RI that is shown in table.3.

Table 3. The Index of Consistency from 1-9 Orders

order	1	2	3	4	5	6	7	8	9
RI	0.00	0.00	0.58	0.90	1.12	1.24	1.32	1.41	1.45

2.2. Calculating the Largest Eigenvalue and Eigenvector

We apply the approximate method to calculate for simply calculation. There are two methods: One is the sum and product methodand the other one is the root method. Sum and product method :

(1) Normalizing each line in the judgment matrix.

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$$a_{ij} = a_{ij} / \sum_{k=1}^{n} a_{kj}$$
 $(i = 1, 2, \cdots, n)$

(2) Summing each line after normalization

$$\overline{\omega}_{i} = \sum_{j=1}^{n} a_{ij}$$
 (j = 1, 2, ..., n)

(3) Normalizing the vector quantity $\overline{\omega} = [\overline{\omega}_1, \overline{\omega}_2, \cdots, \overline{\omega}_n]$

$$\omega = \frac{\overline{\omega}_i}{\sum_{j=1}^n \overline{\omega}_i}, i = 1, 2, \cdots, n$$

 ω is eigenvector

Root method:

(1) The factors in the judgment matrix multiply by row

$$U_{ij} = \prod_{j=1}^{n} a_{ij}$$

(2) Turning evolution for products respectively

$$u_i = n \sqrt{u_{ij}}$$

(3) Normalizing the vector quantity

$$\omega_i = \frac{u_i}{\sum_{i=1}^n u_i}$$

 ω_i is eigenvector

(4) Calculating the largest eigenvalue

$$\lambda_{\max} = \sum_{i=1}^{n} \frac{(A\omega_i)}{n\omega_i}$$

3. The Study on the New Modified AHP Algorithm

3.1. The Revise of the Judgment Matrix

If the elements in the judgment matrix meet $a_{ij} > 0, a_{ij} = \frac{1}{a_{ji}}, a_{ii} = 1(i, j = 1, 2, \dots, n)$, the

matrix *A* is called the positive reciprocal matrix.

Definition 1 We assume the judgment matrix is $A = (a_{ij})_{n \times n}$. If $\forall i, j, k = 1, 2, \dots, n$, there is $a_{ij} = a_{ik}a_{kj}$. We can call the judgment matrix A as the consistent matrix.

The consistent matrix has several properties as follows.

Theorem 1 The sufficient and necessary condition for judging $A = (a_{ij})_{n \times n}$ with the characteristic of the consistency is that the maximum eigenvalue of the matrix A is $\lambda_{max} = n$. The normalized feature vector $\tilde{\omega} = (\tilde{\omega}_1, \tilde{\omega}_2, \cdots, \tilde{\omega}_n)^T$ is the weight vector.

Theorem 2 The sufficient and necessary condition for judging $A = (a_{ij})_{n \times n}$ with the characteristic of the consistency is that there has $a_{ij} = a_{ik}a_{kj}$ for $\forall i, j, k = 1, 2, \dots, n$.

From the definition 1 and the theorem 2, if the positive reciprocal matrix A is the consistent matrix, there must have

$$\forall i, j, k = 1, 2, \cdots, n, a_{ij} = a_{ik} a_{kj}.$$
(1)

We can get the sum for k from formula 1.

$$a_{ij} = \frac{1}{n} \sum_{k=1}^{n} a_{ik} a_{kj}$$
(2)

If the positive reciprocal matrix A is the consistent matrix, the sufficient and necessary condition is formula (1). And the formula (2) is the necessary condition. That is, if the formula (2) is not infringement, the matrix A may be not the consistent matrix. Therefore, the formula (2) is the precondition for judging the consistent matrix. We construct:

$$b_{ij} = \begin{cases} \frac{1}{n} \sum_{k=1}^{n} a_{ik} a_{kj} & i < j \\ 1 & i = j \\ \frac{1}{b_{ij}} & i > j \end{cases}$$
(3)

If $A = (a_{ij})_{n \times n}$ is not satisfied with the consistency, we use $B = (b_{ij})_{n \times n}$ as the modified matrix for the matrix *A*. It improves the possibility to meet the consistency. If *A* is a consistent matrix, B = A.

3.2. The Improved Consistent Test

The maximum eigenvalue of the matrix A is λ_{max} . We assume that $\tilde{\omega}$ is the corresponding and normalized feature vector of the λ_{max} . From the theorem (1), we can know that $\tilde{\omega} = (\tilde{\omega}_1, \tilde{\omega}_2, \cdots, \tilde{\omega}_n)^T$ is the hierarchical single-sort weight vector.

$$A\tilde{\omega} = \lambda_{\max}\tilde{\omega} \tag{4}$$

The matrix *A* is the completely consistent matrix and its maximum eigenvalue is $\lambda_{max} = n$. If *A* does not have the complete consistency, λ_{max} is larger than *n* slightly.

$$||A\tilde{\omega} - \lambda\tilde{\omega}|| = ||A\tilde{\omega} - n\tilde{\omega}|| < \varepsilon$$
(5)

We use formula (5) as the test standard to test the consistency for the matrix A.

From the consistency ratio $CR = \frac{CI}{RI} = \frac{\lambda_{max} - n}{(n-1)RI} < 0.1$ which put forward by the professor T.L.Saaty, we can get:

$$|\lambda_{\max} - n| < 0.1(n-1)RI \tag{6}$$

Putting the formula (6) into $||A\tilde{\omega} - n\tilde{\omega}|| = |\lambda_{\max} - n|^{\circ} ||\tilde{\omega}|| \le |\lambda_{\max} - n|$ we get the formula as follows.

$$\varepsilon = 0.1(n-1)RI \tag{7}$$

$$|\tilde{A\omega} - n\tilde{\omega}| < 0.1(n-1)RI$$
(8)

We use formula (8) to test the satisfactory consistency of the matrix. It can omit to solve the eigenvalue of the matrix A. We only need to calculate the ranking vector. It simplifies the operation and enhances the running speed.

3.2.1. The Consistent Test Sample of the Matrix: We know that

$$A = \begin{vmatrix} 1 & 8 & 9 \\ 1 & 8 & 9 \\ 1 & 1 & 9 \\ 1 & 1 & 9 \\ 1 & 1 & 1 \\ 9 & 1 & 9 \\ 1 & 1 & 1 \end{vmatrix}$$

We get the normalized feature vector by using the square method.

$$\tilde{\omega} = \begin{vmatrix} 0.715 \\ 0.245 \\ 0.040 \end{vmatrix}$$

and

$$\varepsilon = 0.1(n-1)RI = 0.116$$
.

However, $||A\tilde{\omega} - n\tilde{\omega}|| = ||A\tilde{\omega} - 3\tilde{\omega}|| = 1.161 > 0.116$ is not satisfied with the formula (8). Therefore, the matrix does not have the satisfactory consistency. According to the formula (3) we revise the matrix A and get the following matrix.

$$B = \begin{bmatrix} 1 & 17/3 & 30 \\ 3/1 & 1 & 51/8 \\ 1/3 & 8/5 & 1 \end{bmatrix}$$

The normalized eigenvector is

$$\tilde{\omega}^* = \begin{bmatrix} 0.820 \\ 0.154 \\ 0.026 \end{bmatrix}$$

The tested formula is $||B\tilde{\omega}^* - n\tilde{\omega}^*|| = ||B\tilde{\omega}^* - 3\tilde{\omega}^*|| = 0.013 < 0.116$. Therefore, the revised matrix has the characteristic of the satisfactory consistency.

3.2.2. The Calculated Steps of the MCAHP Algorithm: The first step is analyzing problems and establishing a hierarchical analysis model. The model contains the target layer, the attribute layer and the scheme layer.

The second step is adopting the $1\sim9$ scaling method that is proposed by professor T.L.Saaty to construct the judgment matrix at each layer.

The third step is using the square root method to calculate the priority weights of each layer elements.

The fourth step is using the formula (8) to test the consistency of the judgment matrix. If the matrix meets the consistency, we execute the fifth step. If the matrix does not meet the consistency, we revise the judgment matrix by using the formula (3) and execute the third step.

The fifth step is calculating the total order weighs of each scheme.

$$\tilde{\omega}_i = \sum_{j=1}^m \tilde{\omega}_j \omega_i^j$$

Among them, $\tilde{\omega}_i^{j}$ is the ranking weight of the scheme *i* in attribute *j*. $\tilde{\omega}_j^{c}$ is the weight of the attribute *j*. *m* is the number of the attributes.

4. The Exploration of the MCAHP Algorithm

Compared with the original AHP algorithm, the MCAHP algorithm in this paper is simpler. The MCAHP algorithm revises the judgment matrix which cannot satisfy the consistency. Therefore, the new algorithm avoids the progress of reinvestigation. And it also collects data and constructs the judgment matrix while it shortens the needed time to resolve the problems. In addition, it also saves the manpower and the financial resources. Because of the improvement of the consistency criterion, we can use the solved normalized feature vector and the matrix directly to judge the consistency. The MCAHP algorithm avoids the calculation of the maximum eigenvalue.

After a lot of practices prove, the MCAHP algorithm only needs one-time revise. So it satisfies the consistent condition for the judgment matrix which cannot meet the consistency. After one-time revises, we can revise the matric again according to the improved AHP algorithm if the matrix still cannot satisfy with the consistency. In general, an algorithm can terminate running and get an effective result after the finite times(less 20 times).

In this paper, the improved algorithm can also apply the exponential scale method, three standard method ([0,1,2]) and other methods. It is also valid for revising the judgment matrix and tests the consistency. The operation results of the MCAHP algorithm are the same with the original AHP algorithm results.

5. Using the MCAHP Algorithm to Ensure the Weight of the Sports Test Course Achievement Evaluation

We establish the index system for ensuring the physical examination course (figure 2) through extensively collecting the opinions of the experts, teachers and students. We select the pairwise comparison method to construct the judgment matrix at each level by providing a large number of questionnaires. For different judgment matrixes that are obtained from the same index, we use the geometric mean method to get the comprehensive judgment matrix of the index. At last, we use the MCAHP algorithm to solve the weights of each index in this paper. The total order weight is shown in Figure 2.



Figure 2. The Physical Examination Course Achievement Evaluation Index System and the Total Order Weights

Teacher	Attendance	Enthusiasm	Complete	The	$\tilde{\omega}_{i}^{1}$
evaluation	inspection	in sports	the required dives	finial exam	
Attendance inspection	1	0.143	0.333	0.200	0.063
Enthusiasm in sports	7	1	2.333	1.400	0.438
Complete the required dives	3	0.429	1	0.800	0.188
The finial exam	5	0.714	1.667	1	0.313

Table 4. The Teachers' Evaluation Matrix at Scheme Layer

Table 5. The Self-evaluation Matrix at Scheme Layer

Self evaluation	The love of the	Classroom	Extra Physical	$\tilde{\omega}_{_{i}}^{_{2}}$
	sport	lectures	exercise after class	
The love of the	1	0.500	0.333	0.441
sport				
Classroom lectures	2	1	5	0.502
Extra physical	3	0.200	1	0.057
exercise after class				

Table 6. The Peer-evaluation Matrix at Scheme Layer

Peer evaluation	Learning attitude	Cooperation spirit	$\tilde{\omega}_{i}^{3}$
Learning attitude	1	2	0.667
Cooperation spirit	0.500	1	0.333

Table 7. The Judgment Matrix at Attribute Layer which Relatives to theTarget Layer

С	Teacher evaluation	Self evaluation	Peer evaluation	$\tilde{\omega}_{i}^{c}$
Teacher	1	3	3	0.600
evaluation				
Self evaluation	0.333	1	1	0.200
Peer evaluation	0.333	1	1	0.200

Among them, the relative attributive judgment matrix of the student self-assessment is A_2 . The hierarchical single sequencing vector $\tilde{\omega}_2 = (0.156, 0.607, 0.237)^T$, $|| A_2 \tilde{\omega}_2 - n \tilde{\omega}_2 || = 0.382 > 0.1(n-1)RI = 0.116$ is not satisfied with the consistency. The hierarchical single sequencing weight $\tilde{\omega}_i^2 = (0.441, 0.502, 0.057)^T$, $|| B_2 \tilde{\omega}_i^2 - n \tilde{\omega}_i^2 || = 0.022 < 0.116$ which corresponds to the modified matrix B_2 is satisfied with the consistency.

From the sequencing results, we can see that the main factors which affect the performances are the enthusiasm in sports and the final exam. The influences of the attendance inspection and completing the required dives are weaker. This result is same to the original AHP algorithm basically. However, the running speed of the MCAHP

algorithm is faster while it keeps the original data which are provides by the experts at the maximum.

6. Conclusion

Compared with the traditional culture education, the physical education attends classes outside in most cases. In addition, the number of inspection is less than the traditional culture education. Due to the particularity of the physical education, it becomes a key factor to judge the weights of the student physical test course achievement evaluation indexes.

Because the subsystem of the sports management system is affected by many factors, using the analytic hierarchy process has obvious advantages. The analytic hierarchy process requirements the data little accurate and its calculation is simple. It is suitable for solving the decision-making problems which are difficult to analyze by using the quantitative method. AHP is an effective tool to achieve the scientific decision for the complex society and the economic system.

In this paper, we apply the MCAHP proposes to determine the index weights of student examination course evaluation. This method enhances the possibility of the consistency for the judgment matrix and the universality of the sequencing results application. The use of the new improved AHP algorithm provides the scientific index system and the weights for the evaluation of the test course achievement conveniently. The improved algorithm can also be applied to other weight decision problems. This new method has a broad development space and an applicable prospect.

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