

Comprehensive Evaluation of Transformer Condition Based on Fuzzy Grey Clustering and Variable Weight

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Abstract

Aiming at the problem that the transformer condition evaluation factors have fuzzy and gray characteristics and fixed weight (FW) can not accurately evaluate the condition, we proposed a condition evaluation method for transformer based on fuzzy grey clustering and variable weight. The method is applied to evaluate transformer condition layer by layer. Firstly, the confidence degree of the association rules is introduced to determine the FW of key indicators. According to the classification of transformer state grade, the triangle whiten function is established. The grey clustering coefficient (GCC) matrix and fault layer evaluation results are obtained through grey clustering method. Then the variable weight (VW) is obtained by combining variable weight synthesis mode, and then the transformer condition is evaluated by fuzzy evaluation method. The transformer test report data is carried out as case analysis and the result shows that the method we proposed can assess the transformer condition objectively and accurately.

Keywords: transformer; fuzzy grey clustering; fixed weight; variable weight; comprehensive evaluation

1. Introduction

Condition evaluation of electric power equipment is the key link in the process of condition maintenance. Power transformer as one of the most important power equipment, its condition evaluation result directly affects the implementation of maintenance work. Therefore, the transformer condition evaluation method has become a hot research topic [1-2].

At present, the intelligent method is used to evaluate the transformer condition in home and abroad. For example, references [3-4] proposed the grey hierarchy evaluation method. This method adopts correlation analysis to get the correlation degree between different levels, so as to assess the condition. In [5-6], neural network is used to evaluate transformer condition. First, we input transformer information, and then through training this information output the transformer condition. Fuzzy comprehensive evaluation [7-9] method is aimed at the fuzzy characteristic of transformer, using fuzzy mathematics knowledge to get the membership vector, and the condition is obtained by fuzzy composite operation. In [10-11], evidence theory is applied to the transformer condition assessment. There are some literatures through the support vector machine [12-13], matter-element theory [14] and other methods to assess the condition of the transformer.

For above researches, the weight obtained by above methods is fixed weight (FW). But these authors do not consider the problem that when the transformer is abnormal, smaller weight may result in failure to accurately reflect the transformer condition. A determinate state grade boundary is given in [4, 9, 11], but in the actual situation, the boundary is fuzzy, this determinate boundary is not consistent with the actual situation. Transformer

evaluation factor has the characteristics of grey and fuzziness, but literatures [3, 7, 10, 14] only consider the unilateral factor.

For above problems, we proposed the fuzzy grey clustering and variable weight (VW) method for transformer condition evaluation. Firstly, association rules (AR) is introduced to calculate the FW for each key indicator, and the grey clustering analysis (GCA) is used to get the fault layer condition, that is single condition. Then the VW coefficient is obtained by the variable weight synthesis mode, and the transformer condition is evaluated by the fuzzy evaluation method. An example analysis result shows that the evaluation method is valid and practical.

This paper gives a beginning to work in this area. Then the single condition evaluation of transformer is described in Section 2. Section 3 gives the comprehensive condition evaluation method of transformer. In Section 4, a case analysis is discussed. Conclusion remarks are finally offered in Section 5.

2. Single Condition Evaluation of Transformer

When faced with complex evaluation problem, the complex problem can be decomposed into several sub problems, which can simplify the complex problem and improve the accuracy of the evaluation results. The single condition evaluation of transformer is the fault layer evaluation by using GCA method. GCA method not only can avoid the clear division of state grade boundary, but also considers the grey characteristics of transformer.

2.1. Establishment Key Indicator System

According to reference [15] and the strong association feature between fault type and key indicators, the double model key indicator system is constructed, as shown in Figure 1. The first layer is fault layer, which is divided into 8 types of faults, *i.e.*, $FX=\{FX_1, FX_2, \dots, FX_8\}$. The second layer is key indicator layer, *i.e.*, “Moistened insulation” $FX_1=\{FX_{1,1}, FX_{1,2}, \dots, FX_{1,8}\}$.

2.2. Condition Grade Classification and Indicator Unification

In this paper, according to the actual operation situation, the transformer condition is divided into five grades, as shown in Table 1.

Table 1. Condition Grade Classification of Transformer

Condition grade	Transformer condition description
Good	All monitoring data are close to the initial value.
Normal	Monitoring data are far from the attention value.
Attention	Part monitoring data are close to the attention value.
Abnormal	Part monitoring data are close to the warning value.
Fault	Monitoring data exceed the prescribed warning value.

In order to facilitate the comparison and calculation of the key indicators, the original data will be processed, and it's controlled between 0~100, the unified formula is:

$$x_{ij} = \frac{x_z - x_{ij0}}{x_z - x_c} \times 100 \quad (1)$$

Where x_z and x_c denote the warning value and initial value of transformer key indicator. x_{ij0} represents the measured value. When $x_{ij}<0$, lets $x_{ij}=0$, when $x_{ij}>100$, lets $x_{ij}=100$.

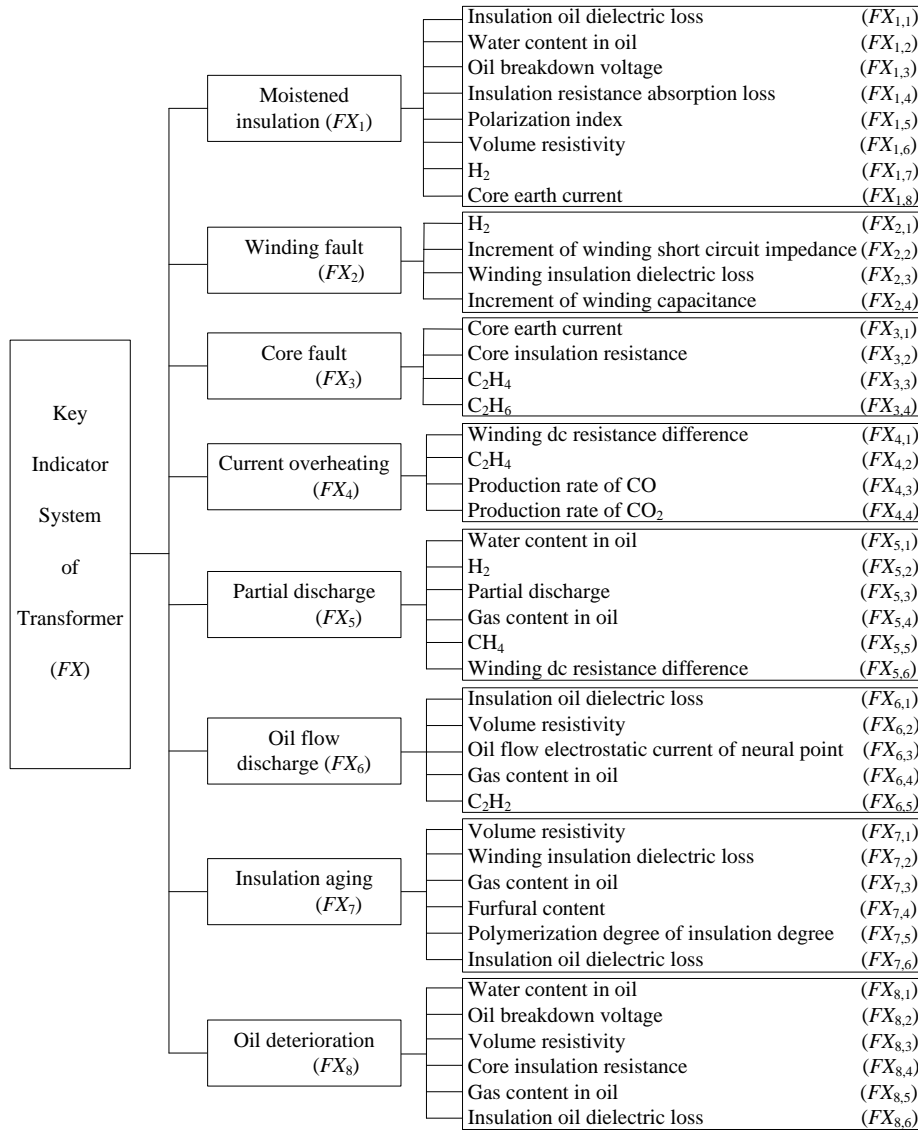


Figure 1. Key Indicator System of Transformer

2.3. Determination of Fixed Weight

AR is used to find all subsets of items or attributes, which appear frequently in the same event [16]. According to the definition of AR, suppose $R=\{\alpha_1, \alpha_2, \dots, \alpha_s\}$ is a finite item set which composed by S item. Given the transaction database (TDB) $M=\{\beta_1, \beta_2, \dots, \beta_N\}$, where $\beta_i=\{\alpha_1, \alpha_2, \dots, \alpha_t\} \subset R$, known as the t-item set. AR reflects the dependence or correlation between the different items, like $X \rightarrow Y$ [support, confidence], where $X \subseteq M, Y \subseteq M$ and $X \cap Y \neq \emptyset$.

Support and confidence are two important concepts in AR. Support degree is the probability that transaction X and Y appear simultaneously in the TDB, that is: $S(X \rightarrow Y) = P(X \cup Y)$. Confidence is the probability of both X and Y contained in TDB, namely, $C(X \rightarrow Y) = P(X, Y) / P(X) = P(X \cup Y) / P(X)$. The greater value of C indicates the higher relationship between transaction X and Y .

It is known that key indicator and fault has strong correlation, which meets the definition of confidence. Therefore, we use the confidence to calculate the FW, the steps are as follow.

1. Determine the transaction database $M = \{\text{transformer appears any fault}\}$.
2. Determine the item set $X_{i,j} = \{j\text{-th key indicator abnormal in } i\text{-th fault}\}$.
3. Determine the item set $Y_i = \{i\text{-th fault occurs}\} = M_i$.

$$C(X_{i,j} \rightarrow Y_i) = \frac{P(X \cup Y)}{P(X)} = \frac{\sigma(X_{i,j} \cup Y_i)}{\sigma(X_{i,j})} \times 100\%$$

4. Calculate confidence C : , where $\sigma(A)$ denotes the number of transaction which contains A in M .

$$\omega_{i,j}^0 = C_{i,j} / \sum_{k=1}^n C_{i,k}$$

5. Determine the FW: , which, $C_{i,j}$ represents the confidence of the j -th key indicator in the i -th fault, n is the number of i -th fault.

Each type fault of transformer is equally important to the transformer condition, so the FW of single condition is $\omega_i^0 = 1/n$, in this paper $n=8$, that is $\omega_i^0 = 0.125$.

2.4. Single Condition Evaluation

The key of GCA evaluation model is to establish an effective whitening function. The evaluation model based on triangle whiten function is suitable for solving the clustering problem of less information [17]. Due to each grade boundary point of transformer is not clear, but easier to determine which grade it most likely belongs to. Therefore, this paper selects the center point triangle whiten function, and the triangle whiten function of the first grey class and final grey class is changed to the WF of lower measure and upper measure respectively. The whitening function of each grey class is fault f_j^1 , abnormal f_j^2 , attention f_j^3 , normal f_j^4 , good f_j^5 , the specific form is as follows:

$$f_j^1 = \begin{cases} 0 & x \notin [0, 20] \\ 1 & x \in [0, 10] \\ \frac{20-x}{10} & x \in [10, 20] \end{cases} \quad f_j^2 = \begin{cases} 0 & x \notin [15, 45] \\ \frac{x-15}{15} & x \in [15, 30] \\ \frac{45-x}{15} & x \in [30, 45] \end{cases}$$

$$f_j^3 = \begin{cases} 0 & x \notin [35, 65] \\ \frac{x-35}{15} & x \in [35, 50] \\ \frac{65-x}{15} & x \in [50, 65] \end{cases} \quad f_j^4 = \begin{cases} 0 & x \notin [55, 85] \\ \frac{x-55}{15} & x \in [55, 70] \\ \frac{85-x}{15} & x \in [70, 85] \end{cases}$$

$$f_j^5 = \begin{cases} 0 & x \notin [80, 100] \\ \frac{x-80}{10} & x \in [80, 90] \\ 1 & x \in [90, 100] \end{cases}$$

The grey clustering coefficient (GCC) of each fault is obtained by using the GCA

formula $\delta_i^k = \sum_{j=1}^m f_j^k(x_{ij})\omega_{i,j}^0$. The single condition is determined by the maximum principle method. Among them δ_i^k is GCC, f_j^k denotes whiten function, $\omega_{i,j}^0$ is FW.

3. Comprehensive Condition Evaluation of Transformer

In the comprehensive condition evaluation of transformer stage, if a single condition is abnormal, and its weight coefficient is not great, it may lead to can't reflect the actual operating condition. Therefore, this paper uses the variable weight theory and fuzzy evaluation method to assess the transformer condition which can avoid the occurrence of such problems.

3.1. Calculation of Variable Weight

The core idea of the VW is that the VW changes with the change of state. The VW formula that introduced into the balance function is as followed:

$$\omega_i(x_1, \dots, x_m) = \omega_i^0 x_i^{(\alpha-1)} / \sum_{k=1}^m \omega_k^0 x_k^{(\alpha-1)} \quad (2)$$

Which, ω_i and ω_i^0 are the VW and FW of the i -th fault, m denotes the number of fault, x_i is the score of i -th fault, and $x_i = \omega_{ij}^0 x_{ij}$, α denotes the balance factor. $\alpha > 0.5$ indicates that the balance consideration of fault is not so important. When the serious flaw of fault is ruled out, then $\alpha < 0.5$. $\alpha = 1$ means equal to FW mode. In this paper $\alpha = 0$.

3.2. Comprehensive Condition Evaluation

The comprehensive condition of transformer is obtained by using fuzzy evaluation method, the formula is $B = J \circ \omega$. Where \circ represents the fuzzy operator, the weighted mean model is used in this paper. J is the matrix of GCC, ω is VW. Finally, the maximum principle method is used to determine the transformer overall condition.

4. Case Analysis

4.1. Application of Condition Evaluation Method

Taking a transformer in a certain area as an example, the measured values x_{i0} , warning values x_w and initial values x_c of key indicators are shown in Table 2.

In Figure 1 the "Winding fault FX_2 " is taken as an example to calculate the FW. We collect the data of key indicator which measured in Table 2. The total TDB contains 880 sets of data, including 116 sets of winding fault. In the 116 sets, the exceed standard times of $FX_{2,1}$, $FX_{2,2}$, $FX_{2,3}$ and $FX_{2,4}$ are 102, 112, 108 and 110. In the 880 sets of TDB, the exceed standard times of four key indicators are 396, 115, 237 and 112. That is $\sigma(FX_{2,1})=396$, $\sigma(FX_{2,2})=115$, $\sigma(FX_{2,3})=237$, $\sigma(FX_{2,4})=112$, $\sigma(FX_{2,1} \cup FX_2)=102$, $\sigma(FX_{2,2} \cup FX_2)=112$, $\sigma(FX_{2,3} \cup FX_2)=108$, $\sigma(FX_{2,4} \cup FX_2)=110$. According to step 4 the

$$C_{2,1} = \frac{\sigma(FX_{2,1} \cup FX_2)}{\sigma(FX_{2,1})} \times 100 = 25.76\%$$

confidence of H_2 is calculated, $C_{2,2}=97.39\%$, $C_{2,3}=45.57\%$, $C_{2,4}=98.21\%$. According to step 5 the FW is computed, $\omega_{2,1}^0=0.0965$, $\omega_{2,2}^0=0.3649$, $\omega_{2,3}^0=0.1707$, $\omega_{2,4}^0=0.3679$. In the same way, the FW of each key indicator is obtained, and the matrix composed of the FW is as following:

$$A = \begin{bmatrix} 0.0654 & 0.0937 & 0.1358 & 0.2632 & 0.2513 & 0.0543 & 0.0601 & 0.0762 \\ 0.0965 & 0.3649 & 0.1707 & 0.3679 & - & - & - & - \\ 0.3857 & 0.1574 & 0.3018 & 0.1533 & - & - & - & - \\ 0.1426 & 0.1475 & 0.3513 & 0.3586 & - & - & - & - \\ 0.1402 & 0.0857 & 0.2004 & 0.0859 & 0.3756 & 0.1122 & - & - \\ 0.1216 & 0.1257 & 0.4413 & 0.1354 & 0.1760 & - & - & - \\ 0.0917 & 0.1508 & 0.0923 & 0.2904 & 0.2980 & 0.0768 & - & - \\ 0.1682 & 0.2514 & 0.1401 & 0.1805 & 0.1293 & 0.1305 & - & - \end{bmatrix}$$

Where, A_{ij} represents the FW of the j -th key indicator in i -th fault.

Table 2. Test Data of Key Indicator

Key indicator	Measured value x_{ij0}	Warning value x_z	Initial value x_c
Oil breakdown voltage/kV	56.7	27	58
Water content in oil/(mg/L)	4.5	32.5	3.5
H ₂ /(uL/L)	160	195	7.0
Increment of winding capacitance/%	5.0	6.5	1
Furfural content/(mg/L)	0.008	0.26	0.0
C ₂ H ₆ /(uL/L)	19.7	84.5	2.5
C ₂ H ₄ /(uL/L)	16.3	65	4.6
Gas in the oil/%	1.6	4	1.0
Increment of winding short circuit impedance/%	3.2	4	1.0
Volume resistivity/(10 ⁹ Ω. m)	48	2.3	60
Winding insulation dielectric loss/tg δ%	0.79	1.04	0.17
Winding dc resistance difference/%	3.7	5.2	1
C ₂ H ₂ /(uL/L)	0	6.5	0.0
Insulating oil dielectric loss/tg δ%	1.46	5.2	0.55
CH ₄	27.3	130	8.5
Insulation resistance absorption loss/%	1.75	1	2
Polarization index	2.16	1.2	2.4
Core earth current/A	0.06	0.13	0.01
Core insulation resistance/MΩ	800	77	1000
Production rate of CO/(%/month)	20	130	0
Production rate of CO ₂ /(%/month)	51	260	0
Partial discharge/pC	67	650	30
Polymerization degree of insulating paper	850	192	1000
Oil flow electrostatic current of neural point/uA	0.08	1.3	0.02

The data in Table 2 are put into formula (1), and then the GCC and cluster results are shown in Table 3. The GCC matrix J is shown as following:

Table 3. GCC and Clustering Results of Single Condition

Single condition	Fault	Abnormal	Attention	Normal	Good	Results
Moistened insulation	0.0088	0.0141	0.0339	0.3171	0.2323	Normal
Winding fault	0.0142	0.7639	0	0	0	Abnormal
Core fault	0	0	0.1723	0.3059	0.0083	Normal
Current overheating	0	0.0878	0.0067	0.1713	0.1797	Good
Partial discharge	0.0126	0.0893	0.0053	0.0286	0.5096	Good
Oil flow discharge	0	0	0	0.1308	0.6225	Good
Insulation aging	0	0.1381	0	0.1603	0.3366	Good
Oil deterioration	0	0	0	0.2173	0.4252	Good

$$J = \begin{bmatrix} 0.0088 & 0.0141 & 0.0339 & 0.3171 & 0.2323 \\ 0.0142 & 0.7639 & 0 & 0 & 0 \\ 0 & 0 & 0.1723 & 0.3059 & 0.0083 \\ 0 & 0.0878 & 0.0067 & 0.1713 & 0.1797 \\ 0.0126 & 0.0893 & 0.0053 & 0.0286 & 0.5096 \\ 0 & 0 & 0 & 0.1308 & 0.6225 \\ 0 & 0.1381 & 0 & 0.1603 & 0.3366 \\ 0 & 0 & 0 & 0.2173 & 0.4252 \end{bmatrix}$$

According to equation (2), the VW vector is $\omega = \{0.1029, 0.2995, 0.1110, 0.1020, 0.1033, 0.0876, 0.1021, 0.0916\}$. The transformer comprehensive condition is obtained by fuzzy evaluation method, and the fuzzy comprehensive evaluation results of FW and VW are shown in Table 4.

Table 4. FW and VW Fuzzy Comprehensive Evaluation Results of Transformer

Weight mode	Fault	Abnormal	Attention	Normal	Good	Result
Fixed weight	0.0045	0.1367	0.0273	0.1664	0.2893	Good
Variable weight	0.0065	0.3384	0.0238	0.1347	0.2236	Abnormal

It can be seen from Table 4, there are significant differences between FW and VW evaluation results, and their results are “Good” and “Abnormal” respectively. But Table 3 clustering results show that the “Winding fault” is abnormal. When power-cut detection, it was discovered that the short circuit has occurred. This leads to the winding fault. Therefore, the transformer condition is abnormal. This shows that the VW fuzzy evaluation result is consistent with the actual situation. It is proved that the evaluation method proposed in this paper can accurately and objectively evaluate the transformer condition.

4.2. Discussion

From the clustering results of single condition, the method proposed in this paper can accurately assess the transformer single condition. This is because that we use the confidence to get the weight, and then combine with the GCA to evaluate the transformer single condition. The method avoids the problems that over-reliance on expert opinion or subjective experience and the difficulty of condition grade boundary division. The method not only gives full play to the advantages of confidence can reflect the FW of each single condition based on objective facts, but also make full use of the advantage of GCA can get each single condition, so as to evaluate the transformer single condition accurately and objectively. In the transformer comprehensive evaluation stage, it can be known that the

VW can accurately reflect the condition of transformer through the comparison results of fixed weight and variable weight evaluation. It is because that the VW can automatically adjust the weight according to the evaluation results of single condition. From the variable weight vector, it can be seen that the single condition weight of non-normal is larger, which highlights the advantages of VW. In summary, the condition method based on fuzzy grey clustering and variable weight can accurately assess the transformer comprehensive condition. And it shows that the method has the theoretical and practical application value.

5. Conclusions

The contributions of this paper are summarized as following:

1. In this paper, we propose a condition evaluation method for transformer based on fuzzy grey clustering and variable weight. The fuzzy grey clustering method not only takes into account the fuzziness of the transformer system, but also considers the characteristics of its grey. The combination of FW and VW makes the evaluation method more reasonable.

2. The double key indicator system of transformer based on fault type is established. Grey clustering method is used to get the single condition of transformer, and then the VW is applied to fuzzy method to evaluate the comprehensive condition. The evaluation method of layer by layer makes the evaluation be logicity, accuracy and practicality.

3. The experimental results show that the proposed method not only can accurately assess the status of the transformer, but also can further determine the cause of the state, which has verified the rationality and practicability of the method.

In the future work, we plan to consider more predict variables that can intervene to improve the clustering quality. And more, for a lot of data information, computer programming should be used.

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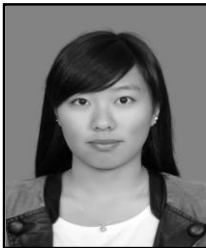
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