

# An Secure Hierarchical Key Agreement Scheme for Wireless Sensor Networks

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## **Abstract**

*In Wireless Sensor Networks (WSN), a key agreement scheme is an essential task for secure communications. Recently, Lee and Kim proposed a hierarchical key agreement scheme for the fresh key establishment in WSN. This scheme achieves a secure session key agreement. In this paper, we analyze the security of the scheme and illustrate that their scheme is unconfident against the insider attack in practice. Moreover, it is also difficult to resist the replay attack in this scheme. Then, we proposed a novel scheme inspired by their scheme. The entities of our scheme include a Sink besides the sensor nodes, which interrupts the construction of the insider attack. Our scheme adopts the timestamp mechanism to resist replay attack, which could decrease the storing requirement of the sensor nodes. Thus, it is more practical and realistic. We illustrate that our proposal can provide stronger security than Lee and Kim's scheme.*

**Keywords:** *Security, Key Agreement Scheme, Wireless Sensor Networks (WSN), Authentication*

## **1. Introduction**

The more wireless sensor technology is being developed, the more benefits are brought to civilian and military requirements by using the Wireless Sensor Networks (WSN). WSN has become a network of integrated sensor technologies, and supports multiple extensible applications, such as emergency response, medical monitoring and battlefield management [1-3]. At the same time, WSN has also attracted various attacks due to the significance of its data [4]. Therefore, how to make the session key agreement securely and efficiently between any two leaf nodes in the open networks becomes a primary security issue [5-7]. The essence of the problem is to implement a hierarchical key agreement scheme [8-10].

In recent years, many security schemes have been proposed for WSN likely environments [6]. In the early days, the public key cryptography (PKC) is the primary solution in WSN as well as other cryptography system [11-14]. Due to the reliability and the credibility of the traditional pair-wise key establishment techniques, the methods are widely cognitive. In particular, the schemes were proposed by using elliptic curve cryptography (ECC) because of the storage and computing cost advantages [15-17]. With the development of identity-based cryptography (IBC) [18] and applications [19, 20], some papers [21-23] have used IBC and pairing-based cryptography for key distribution in WSN.

Recently, Inspired by the Guo *et al.*'s research [8], Kim proposed a hierarchical key agreement protocol applicable to WSN [24]. The scheme is also based on IBC, and claims that it resists the corruption of any sensor nodes in the pyramid. Unfortunately, Lee and Kim found that the scheme in [24] fail to achieve freshness of the session key. Also, Lee and Kim proposed an improved scheme to satisfy the freshness by using the nonce [7] and inherit the security advantages from the paper [24].

In this paper, we show that Lee and Kim's scheme [7] failed to resist the replay attack and the insider attack in practice. We start from constructing a realistic security model. Then, we analyze that the scheme is vulnerable to the replay attack in our security model because the security assumption is too hard to achieve in practice. Moreover, the scheme is hard to resist the insider attack. An adversary, as a cluster head (CH) or a cluster member (CM), could legally acquire the private key, and launch an attack, successfully. In order to resist the attacks, we propose a novel hierarchical key agreement scheme in WSN. Our scheme keeps the quality of key freshness in Lee and Kim's scheme and overcomes the weaknesses of the scheme in our security model.

The remainder of this paper is organized as follows. Section 2 gives the problem characteristics and notations. Section 3 briefly reviews the Lee and Kim's scheme. Section 4 illustrates the drawbacks of their scheme in our security model. Section 5 provides a novel scheme. Section 6 gives a security and performance analysis of our proposed scheme. Finally, the conclusion is presented in Section 7.

## 2. Preliminaries

In this section, we describe the basic system model in WSN and the mathematical backgrounds in our paper. Basic notations are provided at the end of the section.

### 2.1. Basic System Model

A typical WSN configuration involves three parties [25], namely a Sink, the Cluster Heads (CH), and the Cluster Members (CM). We assume there are  $n$  CHs, namely  $\{CH_i\}_{i=1}^n$ . Every CH whose identity is  $CH_i$  manages  $m$  CMs, namely  $\{CM_{ij}\}_{j=1}^m$ . All CMs communicate with others through their CH and the Sink. Figure 1 illustrates the basic system model of the WSN.

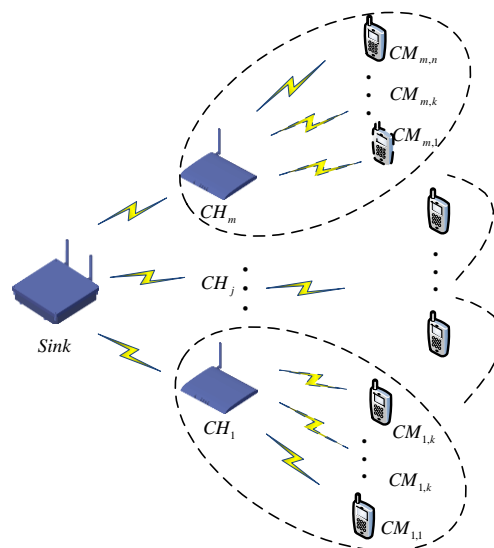


Figure 1. Basic System Model of WSN

## 2.2. Mathematical Backgrounds

### 2.2.1. Bilinear Maps

Let  $G_1$  and  $G_2$  be two cyclic groups of prime order  $P$ , and Let  $P$  be a generator of  $G_1$ . The bilinear pairing is a map  $\hat{e}: G_1 \times G_1 \rightarrow G_2$  with following properties.

**Bilinearity.** For all  $P, Q \in G_1$  and  $a, b \in Z_q^*$ ,  $\hat{e}(aP, bQ) = \hat{e}(P, Q)^{ab}$ .

**Non-degeneracy.**  $\hat{e}(P, P) \neq 1$ .

**Computability.** For all  $P, Q \in G_1$ , we can find an efficient algorithm to compute  $\hat{e}(P, Q)$ .

### 2.2.2. Discrete Logarithm Problem

Given a randomly chosen  $h = aP$  and  $P$  in an additive cyclic group  $G_1$ , with  $a \in Z_q^*$ , compute  $a \in Z_q^*$ . We say that the  $(t - \varepsilon)$ -DLP assumption holds in  $G_1$  if on  $t$ -time algorithm has non-negligible advantage  $\varepsilon$  in solving the Discrete Logarithm Problem (DLP) in  $G_1$ .

## 2.3. Notations

To provide a quick reference, the basic notations used in this paper are listed in Table 1.

**Table 1. Basic Notations**

Notations	Descriptions
$CH_i$	The cluster head $i$
$CM_{ij}$	The cluster member node $j$ in the cluster head $i$
$ID_i$	The identity of $i$
$AD_i$	The amplified identity of $i$
$H_1(\cdot)$	The hash function, which maps $\{0,1\}^* \rightarrow G_1$
$H_2(\cdot)$	The hash function, which maps $G_2 \times G_1^2 \times \{0,1\}^n \rightarrow \{0,1\}^n$
$H_3(\cdot)$	The hash function, which maps $G_1^4 \times \{0,1\}^{2n} \rightarrow \{0,1\}^n$
$T_i$	The $i$ -th timestamp

## 3. Review of the Scheme in Paper

In this section, we briefly review the Lee and Kim's freshness consideration key agreement scheme in paper [7], which consist of two phases: Hierarchical Key Settlement Phase, Session Key Agreement and Secure Communication Phase. It is assumed that each entities shares two groups  $G_1$  and  $G_2$  of prime order  $P$  with a bilinear map  $\hat{e}: G_1 \times G_1 \rightarrow G_2$  and a cryptographic hash function  $H: \{0,1\}^* \rightarrow G_1$ . The basic transmission of the scheme is shown in Figure 2.

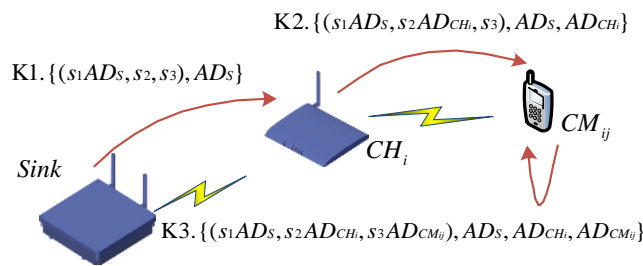
### 3.1. Hierarchical Key Settlement Phase

**Step K1.** Sink picks three random numbers  $s_1, s_2, s_3 \leftarrow Z_q^*$  as the master private keys. Then, Sink computes an amplified identity  $AD_s = H(ID_s)$  and a public key  $s_1 AD_s$ ,

where  $ID_S$  is the real identity of Sink. Then, Sink secure stores the master private key  $(s_1, s_2, s_3)$  and the amplified identity  $AD_S$ . Finally, Sink sends the data package  $\{(s_1 AD_S, s_2, s_3), AD_S\}$  to the CH via a secure way.

**Step K2.** After CH ( $ID_{CH_i}$ ) receives the package, it computes  $AD_{CH_i} = H(ID_{CH_i})$  and  $s_2 AD_{CH_i}$ . Then, CH secure stores the private key  $(s_1 AD_S, s_2, s_3)$  and the amplified identities  $(AD_S, AD_{CH_i})$ . Finally, CH sends the data package  $\{(s_1 AD_S, s_2 AD_{CH_i}, s_3), AD_S, AD_{CH_i}\}$  to its member nodes  $\{CM_{ij}\}_{j=1}^m$  via a secure way.

**Step K3.** After the CM ( $ID_{CM_{ij}}$ ) receives the package, it computes  $AD_{CM_{ij}} = H(ID_{CM_{ij}})$  and  $s_3 AD_{CM_{ij}}$ . Then, CM secure stores the private keys  $(s_1 AD_S, s_2 AD_{CH_i}, s_3 AD_{CM_{ij}})$  and the amplified identity  $(AD_S, AD_{CH_i}, AD_{CM_{ij}})$ , respectively.



**Figure 2. Hierarchical Key Settlement Phase of the Scheme**

### 3.2. Session Key Agreement and Secure Communication Phase

Two CMs ( $CM_{ij}$  and  $CM_{kl}$ ) compute a session key as follows.

**Step C1.** The CM ( $CM_{ij}$ ) chooses a random number  $r_1$ , and computes  $R_1 = r_1 AD_{CM_{ij}}$ . The session key  $sk$  is given by the following formula. Here  $AD_{S'} = H(ID_S)$ ,  $AD_{CH_k'} = H(ID_{CH_k})$  and  $AD_{CM_{kl}'} = H(ID_{CM_{kl}})$ .

$$sk = \hat{e}(s_1 AD_S, AD_{S'}) \cdot \hat{e}(s_2 AD_{CH_i}, AD_{CH_k'}) \cdot \hat{e}(s_3 AD_{CM_{ij}}, AD_{CM_{kl}'})^{r_1} \quad (1)$$

Then,  $CM_{ij}$  computes the verifier  $V_1 = H(sk, R_1)$ , and sends the data package  $\{R_1, V_1\}$  to the other CM ( $CM_{kl}$ ).

**Step C2.** After  $CM_{kl}$  receives the package, it computes the session key  $sk^*$  by the following formula, where  $AD_{S'} = H(ID_S)$  and  $AD_{CH_i'} = H(ID_{CH_i})$ .

$$sk^* = \hat{e}(s_1 AD_S, AD_{S'}) \cdot \hat{e}(s_2 AD_{CH_i}, AD_{CH_i'}) \cdot \hat{e}(s_3 AD_{CM_{kl}}, R_1) \quad (2)$$

Then,  $CM_{kl}$  also computes the verifier  $V_1^* = H(sk^*, R_1)$ . Only if  $V_1^*$  is equal to  $V_1$ ,  $CM_{kl}$  assures the correctness of  $sk^*$ .

**Step C3.** After  $CM_{kl}$  assures the session key  $sk^*$ , it encrypts the plain data  $DATA$  to get the encrypt data  $EDATA$  by using the key. Then,  $CM_{kl}$  computes the verifier  $V_2 = H(sk^*, EDATA)$ , and sends the data package  $\{EDATA, V_2\}$  to  $CM_{ij}$ .

**Step C4.** After  $CM_{ij}$  receives the package, it also computes the verifier  $V_2^* = H(sk, EDATA)$ . Only if  $V_2^*$  is equal to  $V_2$ ,  $CM_{ij}$  assures the correctness of the encrypt data  $EDATA$  and the session key  $sk$ .

## 4. Cryptanalysis of Lee and Kim's Scheme

In this section, we propose a more practical security model. Moreover, we point out Lee and Kim's scheme [7] suffers two attacks in our model. The details are explained in the following section.

### 4.1. Our Security Model

The authors of the paper proposed a hierarchical key agreement scheme in WSN. The authors assume the insider's secret values are reliable and security, such as the private key of the CHs and the CMs. The adversary can only implement the active and passive attack by controlling the insecurity channel. However, it is more useful to carefully consider the corruption risk of the internal nodes. In practice, the WSN is easily attacked from inside. For example, the adversary can capture some nodes, and then use the side channel attacks to get the secret values of the nodes. Therefore, we propose a more practical security model.

Inspired by the papers, we enhance the ability of the adversary in our model. Same as others, the adversary can totally control over the communication channel. More precisely, the adversary may eavesdrop, intercept, modify, replay or inject the communication between any entities in the WSN (e.g. the channel between  $CM_{ij}$  and  $CM_{kl}$ ). Furthermore, the adversary can also corrupt some the secret parameters from the CHs and the CMs except those of the entities who are attacking by the adversary. This state imitates that the insider is corrupted in the WSN. Under above conditions, the scheme should have the ability to resist various kinds of attacks, and achieve the following security goals. (1) **Key security**. Any adversary cannot obtain the current session key. (2) **Known-key security**. Any adversary compromised a shared session key cannot obtain the current session key.

### 4.2. Weaknesses

According to Lee and Kim's paper [7], we find that the scheme has the following disadvantages in our security model.

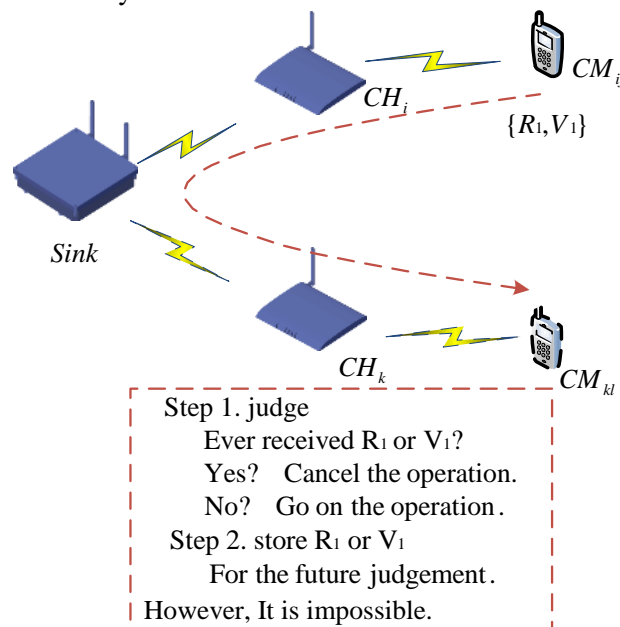


Figure 3. Cannot Resist the Replay Attack

#### 4.2.1. It Cannot Resist the Replay Attack

The scheme will have security problems if the adversary launches the replay attack in real world. As we know, the nonce  $R_1$  is used to prevent the replay attack in the paper. However, the scheme cannot resist replay attack in practice. More precisely, it is essential that the CM should judge whether the nonce  $R_1$  and verifier  $V_1$  have ever received. In order to make a judgment, the CMs should store the received nonce  $R_1$ , interminably. However, it is obviously impossible to sensor nodes because of the limited resources. Thus, it cannot resist the replay attack to use the method in Lee and Kim's scheme. The more details are described as follows.

As is shown in Figure 3, when the adversary has captured the data packet  $\{R_1, V_1\}$  from  $CM_{ij}$  to  $CM_{kl}$ , he/she can store it. Then he/she can replay the nonce  $R_1$  and the verifier  $V_1$  whenever he/she wants. If the victim CM ( $CM_{kl}$ ) receives the data packet  $\{R_1, V_1\}$ , it is obviously that it can believe the package from the real node  $CM_{ij}$  because  $V_1$  is equal to  $H(sk^*, R_1)$ . In order to avoid the attack,  $CM_{kl}$  should be stored the nonce  $R_1$  received before and judge whether the current nonce  $R_1$  is a replay attack. However, there is not enough resource to support the storing and querying nonce in CM. Thus, Lee and Kim's scheme cannot resist the replay attack in practice.

#### 4.2.2. It Cannot Resist the Insider Attack (the Cluster Head Disguise)

We now demonstrate that the Lee and Kim's scheme is vulnerable to the one kind of insider attack. The adversary who has registered as a legal CH ( $CH_A$ ) as shown in Figure 4. According to the definition of our security model, the adversary can intercept the communication data in the WSN because the wireless channel is openness. The adversary who disguises a CH successfully attacks a communication between  $CM_{ij}$  and  $CM_{kl}$  as follows.

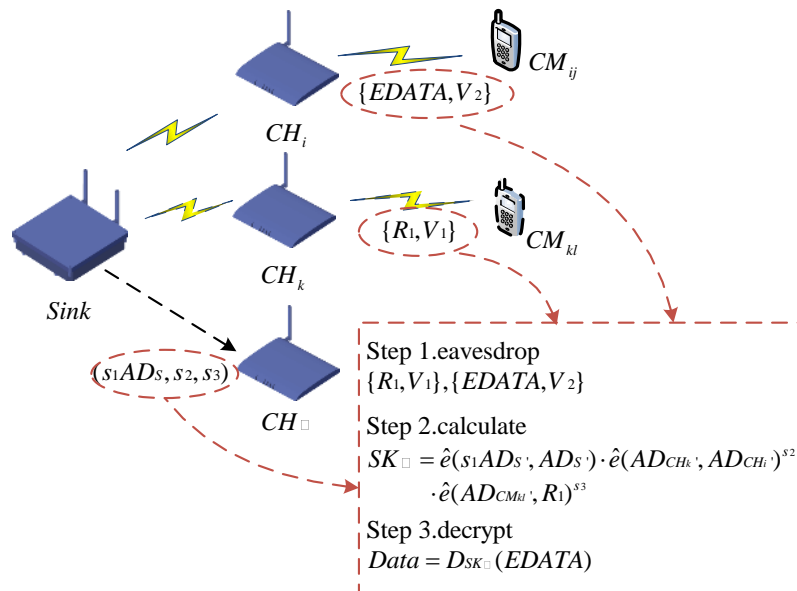


Figure 4. Cannot Against Insider Attack

**Step H1.** Assume that  $CH^A$  is an adversary who has registered as a CH, and then it can legally receive a private key set  $(s_1AD_s, s_2, s_3)$  from the Sink (**Step K1**).

**Step H2.** Suppose  $CM_{ij}$  and  $CM_{kl}$  are victim CMs who send the data packages through their CHs ( $CH_i$  and  $CH_k$ ) and Sink. When  $CM_{ij}$  runs the **Step C1**, the adversary can intercept the data package  $\{R_1, V_1\}$  because channel is unsecure between  $CM_{ij}$  and  $CM_{kl}$ .

**Step H3.** When  $CM_{kl}$  sends back the encrypt data  $EDATA$  to  $CM_{ij}$  at the Step C3, the adversary can also intercept the data package  $\{EDATA, V_2\}$ .

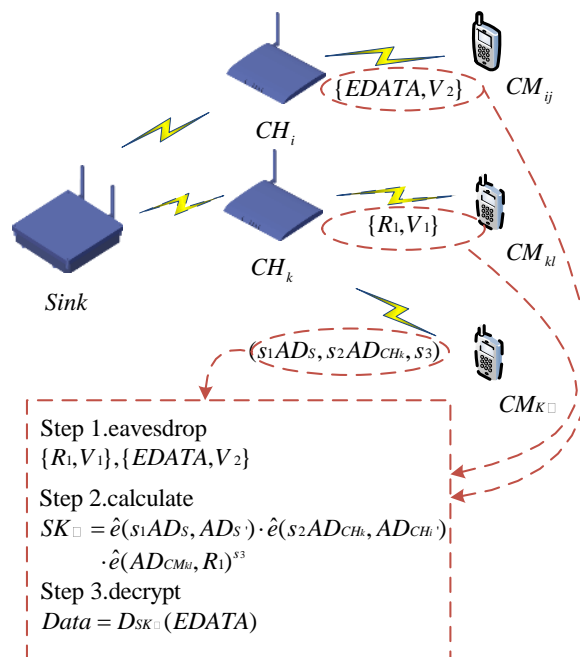
**Step H4.** After the above steps, the adversary  $CH^A$  can compute the key  $sk^A$  by the following formula. Here, the values  $AD_{S'} = H(ID_S)$ ,  $AD_{CH_k'} = H(ID_{CH_k})$ ,  $AD_{CH_i'} = H(ID_{CH_i})$  and  $AD_{CM_{kl}'} = H(ID_{CM_{kl}})$ .

$$\begin{aligned} sk^A &= \hat{e}(s_1AD_s, AD_{S'}) \cdot \hat{e}(AD_{CH_k'}, AD_{CH_i'})^{s_2} \cdot \hat{e}(AD_{CM_{kl}'}, R_1)^{s_3} \\ &= \hat{e}(s_1AD_s, AD_{S'}) \cdot \hat{e}(s_2AD_{CH_k}, AD_{CH_i'}) \cdot \hat{e}(s_3AD_{CM_{kl}}, R_1) \\ &= sk \end{aligned} \quad (3)$$

**Step H5.** The adversary  $CH^A$  can decrypt  $EDATA$  to obtain the encrypt data between  $CM_{ij}$  and  $CM_{kl}$  by using the session key  $sk^A$  because the keys  $sk^A$ ,  $sk$  and  $sk^*$  are equal. Thus, Lee and Kim's scheme [7] cannot resist the insider attack when the adversary disguises a CH.

#### 4.2.3. It Cannot Resist the Insider Attack (the Cluster Member Disguise)

Moreover, there is another insider attack as follows. The adversary who has registered as a legal CM ( $CM_{k^A}$ ) as shown in Figure 5. The adversary has the same CH ( $CH_k$ ) with the one victim  $CM_{kl}$ . Therefore, the adversary is a neighbor node of the victim. The adversary launches an attack to the communication between  $CM_{ij}$  and  $CM_{kl}$  as follows.



**Figure 5. Cannot Against Insider Attack**

**Step M1.** Assume that  $CH^A$  is an adversary who has registered as a CM in a CH ( $CH^k$ ), and then it legally receives a private key set  $(s_1AD_s, s_2AD_{CH^k}, s_3)$  from  $CH^k$  (**Step K2**).

**Step M2.** Suppose two CMs ( $CM_{ij}$  and  $CM_{kl}$ ) are victim nodes. It is same above describe that the adversary can intercept the data  $\{R_1, V_1\}$  and  $\{EDATA, V_2\}$ .

**Step M3.** After the above steps, The adversary  $CH^A$  can compute the session key as follows. Here, the values  $AD_{S'} = H(ID_S)$ ,  $AD_{CH^i} = H(ID_{CH^i})$  and  $AD_{CM_{kl}} = H(ID_{CM_{kl}})$ .

$$\begin{aligned} sk_A &= \hat{e}(s_1AD_s, AD_{S'}) \cdot \hat{e}(s_2AD_{CH^k}, AD_{CH^i}) \cdot \hat{e}(AD_{CM_{kl}}, R_1)^{s_3} \\ &= \hat{e}(s_1AD_s, AD_{S'}) \cdot \hat{e}(s_2AD_{CH^k}, AD_{CH^i}) \cdot \hat{e}(s_3AD_{CM_{kl}}, R_1) \\ &= sk \end{aligned} \quad (4)$$

**Step M4.** It is obviously that the keys  $sk_A$ ,  $sk$  and  $sk^*$  are equal. Therefore, the adversary  $CH^A$  can decrypt  $EDATA$  to obtain the plain text  $DATA$  using the key  $sk_A$ . Thus, Lee and Kim's scheme cannot resist the insider attack when the adversary disguises a neighbor CM with one of two victims.

## 5. Our Enhanced Scheme

In this section, we propose an improved scheme based on identity-based cryptography, which can overcome the weaknesses of Lee and Kim's scheme in Section 4. Our scheme construction is inspired by the papers [7-8, 19]. Our scheme consists of three operational phase: System Parameter Generation Phase, Initial Phase, Authentication and Transmission Phase. The details of our scheme are described as follows.

### 5.1. System Parameter Generation Phase

Similar to the papers [7-8], we use the identity-based encryption (IBE) and the hierarchical structure in our scheme. More specifically, the identity of a sensor node is his/her public key, and his/her private key generates by the Private Key Generator (PKG) in Sink. The parent nodes calculate and release the private key set for their descendants.

**Step G1.** Sink generates two addition groups  $G_1$  and  $G_2$  of prime order  $P$  with a bilinear map  $\hat{e}: G_1 \times G_1 \rightarrow G_2$ . Then, Sink chooses three hash functions satisfied  $H_1: \{0,1\}^* \rightarrow G_1$ ,  $H_2: G_2 \times G_1^2 \times \{0,1\}^n \rightarrow \{0,1\}^n$  and  $H_3: G_1^4 \times \{0,1\}^{2n} \rightarrow \{0,1\}^n$ . After that,

it randomly chooses  $3+m$  random numbers  $\{s_1, s_2, s_3, sr_i \leftarrow Z_q^* \mid i \in (1, \dots, m)\}$  as a master key of Sink and a random generator  $P_0 \in G_1$ . Here,  $m$  is the number of CHs in WSN.

Finally, Sink secure stores the master key  $MK = \{s_1, s_2, s_3, sr_i \leftarrow Z_q^* \mid i \in (1, \dots, m)\}$  and publishes the public parameters  $params = \{q, G_1, G_2, P_0, \hat{e}, H_1, H_2, H_3, s_1P_0, s_2P_0, s_3P_0, sr_iP_0 \mid i \in (1, \dots, m)\}$ .

### 5.2. Initial Phase

**Step I1.** When a CH ( $CH^i$ ) with identity  $ID_{CH^i}$  wants to register in WSN. It sends his identity  $ID_{CH^i}$  to Sink. Sink computes the amplified identities  $(AD_s, AD_{CH^i})$  and the private key  $(s_1sr_i AD_s, s_2sr_i AD_{CH^i}, s_3sr_i)$ . Here, the values  $AD_s = H_1(ID_s)$  and  $AD_{CH^i} = H_1(ID_{CH^i})$ . Then, the Sink sends the data package  $\{(s_1sr_i AD_s, s_2sr_i AD_{CH^i}, s_3sr_i), (AD_s, AD_{CH^i})\}$  to  $CH^i$  via a secure channel. Finally,  $CH^i$  keeps the received information in its secure memory.



**Step I2.** When a CM ( $CM_{ij}$ ) with identity  $ID_{CH_i}$  wants to register in WSN. It sends his identity  $ID_{CM_{ij}}$  to its CH ( $CH_i$ ).  $CH_i$  computes  $AD_{CM_{ij}} = H(ID_{CM_{ij}})$  and  $s_{3SR_i} AD_{CM_{ij}}$ . Then, the CH ( $CH_i$ ) sends the private key set  $\{(s_{1SR_i} AD_s, s_{3SR_i} AD_{CM_{ij}}), (AD_s, AD_{CM_{ij}})\}$  to its CM ( $CM_{ij}$ ), securely. Finally,  $CM_{ij}$  keeps the received information in its secure memory.

### 5.3. Authentication and Key Agreement Phase

When  $CM_{ij}$  wants to establish a session key  $sk$  with  $CM_{kl}$  by the helping of Sink, the following steps are executed among  $CM_{ij}$ ,  $CM_{kl}$  and Sink in Figure 6.

**Step A1.**  $CM_{ij}$  chooses a random number  $r_1$ . Then it computes an amplified identity  $AD_{CM_{kl}} = H_1(ID_{CM_{kl}})$ ,  $R_1 = r_1 AD_{CM_{ij}}$  and  $R_s = r_1 AD_s$ . The temporary key  $k$  is calculated by using the above parameters and the private key set  $(s_{1SR_i} AD_s, s_{3SR_i} AD_{CM_{ij}})$ .

$$k = \hat{e}(s_{1SR_i} AD_s, AD_s)^{r_1} \cdot \hat{e}(s_{3SR_i} AD_{CM_{ij}}, AD_{CM_{kl}})^{r_1} \quad (5)$$

Then,  $CM_{ij}$  computes the verification values  $V_2 = H_2(s_{1SR_i} AD_s, s_{3SR_i} AD_{CM_{ij}}, R_1, R_s, T_1, V_1)$  and  $V_1 = H_2(sk, AD_{CM_{ij}}, AD_{CM_{kl}}, "0")$ . Then it sends  $M_1 = \{AD_{CM_{kl}}, T_1, R_1, R_s, V_1, V_2\}$  to Sink. Here,  $T_1$  is a timestamp.

**Step A2.** After received the data package  $M_1$ , Sink verifies the timestamp  $T_1$  whether it is within the valid time for communication. If it is invalid, the program terminates. Otherwise, Sink judges whether the received  $V_2$  is equal to  $H_2(s_{1SR_i} AD_s, s_{3SR_i} AD_{CM_{ij}}, R_1, R_s, T_1, V_1)$  and computes whether  $\hat{e}(R_s, AD_{CM_{ij}}) = \hat{e}(R_1, AD_s)$ . Only if they are all equal, Sink convince the two values  $R_1$  and  $R_2$ , then it computes  $R_1^* = s_{1SR_i} r_1^{-1} R_1$  and  $R_s^* = s_{1SR_i} r_1^{-1} R_s$ . Otherwise, it ends the processing. Sink computes the value  $V_3 = H_3(s_{1SR_k} AD_s, s_{3SR_k} AD_{CM_{kl}}, R_s^*, R_1^*, T_2, V_1)$ , and sends  $M_2 = \{AD_{CM_{ij}}, T_2, V_1, V_3, R_1^*, R_s^*\}$  to  $CM_{kl}$ .

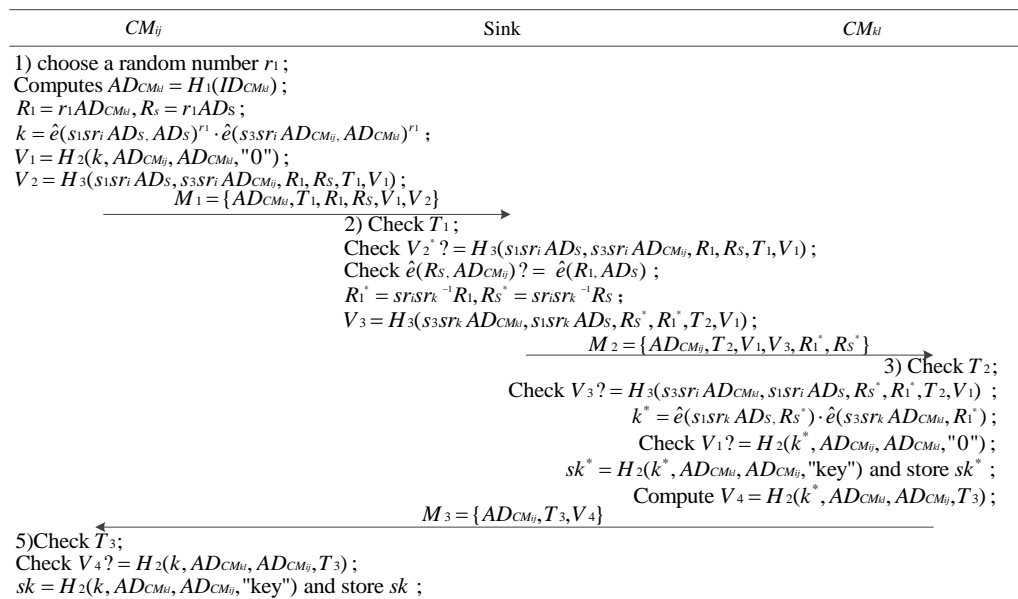


Figure 6. Authentication and Key Agreement Phase in our Scheme

**Step A3.** After received the data package  $M_2$ ,  $CM_{kl}$  checks the validity of the timestamp  $T_2$ . If it has grown stale,  $CM_{kl}$  ends the session. Otherwise, it judges whether the verifier  $V_3$  is equal to the hash value  $H_3(s_1SR_k AD_s, s_3SR_k AD_{CM_{kl}}, RS^*, R_1^*, T_2, V_1)$ . Only if they are equal,  $CM_{kl}$  computes the temporary key  $k^*$  as follows.

$$k^* = \hat{e}(s_1SR_k AD_s, RS^*) \cdot \hat{e}(s_3SR_k AD_{CM_{kl}}, R_1^*). \quad (6)$$

Otherwise, it ends the processing. Then,  $CM_{kl}$  checks whether the received value  $V_1$  is equal to the hash value  $H_2(k^*, AD_{CM_{ij}}, AD_{CM_{kl}}, "0")$ . Only if they are equal,  $CM_{kl}$  authenticates  $CM_{ij}$  and assures the temporary key  $k^*$ . Then,  $CM_{kl}$  computes  $sk^* = H_2(k^*, AD_{CM_{kl}}, AD_{CM_{ij}}, "key")$ , and a value  $V_4 = H_2(k^*, AD_{M_1}, AD_M, \exists T)$ . Finally, it sends  $M_3 = \{AD_{CM_{kl}}, T_3, V_4\}$  to  $CM_{ij}$ . Here,  $T_3$  is a current timestamp.

**Step A4.** After received the data package  $M_3$ ,  $CM_{ij}$  checks the validity of the timestamp  $T_3$ . If it is invalid, it terminates the processing. Otherwise,  $CM_{ij}$  computes a hash value  $V_4^* = H_2(k, AD_{CM_{kl}}, AD_{CM_{ij}}, T_3)$ . Only if  $V_3 = V_4^*$ ,  $CM_{ij}$  computes the session key  $sk$  is equal to  $H_2(k, AD_{CM_{kl}}, AD_{CM_{ij}}, "key")$  with  $CM_{kl}$ .

## 6. Correctness and Security Analysis

In this section, we present the correctness of our improved scheme. Then, we analyze our enhancement scheme regarding security and overcome the weaknesses analyzed in Section 3.

### 6.1. Correctness

We verify the correctness of key agreement in our scheme as follows.

$$\begin{aligned} k &= \hat{e}(s_1SR_i AD_s, AD_s)^{r_1} \cdot \hat{e}(s_3SR_i AD_{CM_{ij}}, AD_{CM_{kl}})^{r_1} \\ &= \hat{e}(s_1SR_i AD_s, r_1 AD_s) \cdot \hat{e}(s_3SR_i AD_{CM_{kl}}, r_1 AD_{CM_{ij}}) \\ &= \hat{e}(s_1SR_i SR_k AD_s, SR_k^{-1} RS) \cdot \hat{e}(s_3SR_i SR_k AD_{CM_{kl}}, SR_k^{-1} R_1) \\ &= \hat{e}(s_1SR_k AD_s, SR_i SR_k^{-1} RS) \cdot \hat{e}(s_3SR_k AD_{CM_{kl}}, SR_i SR_k^{-1} R_1) \\ &= \hat{e}(s_1SR_k AD_s, RS^*) \cdot \hat{e}(s_3SR_k AD_{CM_{kl}}, R_1^*) \\ &= k^* \end{aligned} \quad (7)$$

The session key, computed by  $CM_{ij}$  and  $CM_{kl}$ ,  $sk = H_2(k, AD_{CM_{kl}}, AD_{CM_{ij}}, "key")$  and  $sk^* = H_2(k^*, AD_{CM_{kl}}, AD_{CM_{ij}}, "key")$  are equal.

### 6.2. Security Analysis

#### 6.2.1. Authentication

$CM_{ij}$  sends the data packages  $M_1 = \{AD_{CM_{kl}}, T_1, R_1, RS, V_1, V_2\}$  to Sink. Here, the value  $V_2 = H_2(s_1SR_i AD_s, s_3SR_i AD_{CM_{ij}}, R_1, RS, T_1, V_1)$ . Without the private keys  $s_1SR_i AD_s$  and  $s_3SR_i AD_{CM_{ij}}$ , the adversary cannot generate a legal data package  $M_1$  due to the nature of the hash function. Therefore, Sink could authenticate  $CM_{ij}$  by checking the correctness of the value  $V_2$ . Similarly,  $CM_{kl}$  could authenticate Sink by judging the accuracy of the  $V_3$ . A sensor node  $CM_{kl}$  sends the message  $M_3 = \{AD_{CM_{kl}}, T_3, V_4\}$  to another node  $CM_{ij}$ .

Here, the value  $V_4 = H_2(k^*, AD_{CMkl}, AD_{CMij}, T_3)$ . Since only  $CM_{ij}$  and  $CM_{kl}$  can compute the temporary key  $k^*$ . Therefore,  $CM_{ij}$  could authenticate  $CM_{kl}$  through checking the correctness of the  $V_4$ . It is essential to note that the scheme should ensure adequate entropy of the keys in the System Parameter Generation Phase in order to prevent the offline guessing attack.

### 6.2.2. Security Key Establishment

Key security is a critical requirement for a key agreement scheme. Assume that the adversary succeed get the session key  $sk = H_2(k, AD_{CMkl}, AD_{CMij}, \text{"key"})$  described in Section 5. Since the hash function has the one-way characteristic, the adversary should obtain the temporary  $k$  or  $k^*$  for computing the key  $sk$ . However, the temporary key  $k$  is established by  $CM_{ij}$  in the Step A1. Since the adversary does not know the private values of  $CM_{ij}$ , he/she cannot compute the temporary key  $k = \hat{e}(s_{1SRi} AD_S, AD_S)^{r_1} \cdot \hat{e}(s_{3SRi} AD_{CMij}, AD_{CMkl})^{r_1}$ . Moreover, In the Step A3, the temporary  $k^*$  is established by  $CM_{kl}$ . Since the adversary does not know the values of  $s_{1SRk} AD_S$  and  $s_{1SRk} AD_{CMkl}$  together, he/she cannot calculate the temporary key  $k^*$  by formula  $k^* = \hat{e}(s_{1SRk} AD_S, R_S^*) \cdot \hat{e}(s_{3SRk} AD_{CMkl}, R_1^*)$ .

Our scheme also achieves perfect forward secrecy. Since the numbers of  $R_1$  and  $R_S$  are randomly computed in every communication, the values of  $R_1^*$  and  $R_S^*$  are freshly in every stage. Therefore, all the historical session keys will still secure even if the long-term private keys are disclosed in future. Base on the one-way function and the freshness of  $R_1$  and  $R_S$ , the adversary cannot obtain any information about the future session key even if the current session key  $sk$  or  $sk^*$  is compromised.

### 6.2.3. Security Against Replay Attacks

Our scheme can resist replay attack because we used the timestamps. If an adversary replays the eavesdropped message, then the sensor nodes will detect the attack when examining the current time. During the authentication and key agreement phase, when Sink receives a data package  $M_1 = \{AD_{CMkl}, T_1, R_1, R_S, V_1, V_2\}$ , it verifies the timestamp  $T_1$  with the current time. If the message is a replay message, then Sink will find it. If adversary change the timestamp  $T_1$  in data package  $M_1$ , however, it cannot know the values of  $s_{1SRi} AD_S$ ,  $s_{1SRi} AD_{CMij}$ , Sink will find the replay when it check the value  $V_2$ . Similarly, when  $CM_{kl}$  receives the data package  $M_2 = \{AD_{CMij}, T_2, V_1, V_3, R_1^*, R_S^*\}$ , it judges the timestamp  $T_2$  to against the message replay. Similarly, when  $CM_{ij}$  receives the data package  $M_3 = \{AD_{CMkl}, T_3, V_4\}$ , it resist the message replay by judging the timestamp  $T_3$  and the session key  $sk$ . It is should admit that the synchronization problem is the main vulnerability to timestamp, However, the situation has been released with the development of the sensor technologies [26] such as using the linear regression to achieve long-term synchronization and using the time base signal in the Global Position System (GPS). The timestamp is the economic and effective means to resist the replay attack in WSN.

### 6.2.4. Security Against Insider Attacks

In the proposed scheme, Sink computes and distributes different private keys  $(s_{1SRi}AD_s, s_{2SRi}AD_{CH_i}, s_{3SRi})$  for various CHs. Thus, the adversary CH cannot get the information including the private keys of the other CHs. Furthermore, if we assume that an adversary CM who has registered as  $CM_{ij}$  can obtain  $s_{1SRi}AD_s$  and  $s_{3SRi}AD_{CM_i}$  from  $CH_i$ . However, he/she cannot calculate  $s_{3SRi}$  from  $s_{3SRi}AD_{CM_{ij}}$  except he/she can solve the DLP assumption. Thus, our scheme destructs the attack conditions as **Step H1** and **Step M1**. As a result, the scheme prevents the adversary to generate the temporary key  $k$  and the session key  $sk$  in sequence. Therefore, the proposal could withstand the insider attack. It should be noted that Sink has an enough computing power as a data concentrator node. Although our proposal increases the computation cost of Sink, the advice is feasible to WSN.

### 6.2.5. Security Against Impersonation Attacks

To impersonate  $CM_{ij}$  to Sink, an adversary has to generate a legal message  $M_1 = \{AD_{CM_{ij}}, T_1, R_1, R_s, V_1, V_2\}$ , where  $V_2 = H_2(s_{1SRi}AD_s, s_{3SRi}AD_{CM_{ij}}, R_1, R_s, T_1, V_1)$ . The adversary cannot compute  $V_2$  because the values  $s_{1SRi}AD_s$  and  $s_{3SRi}AD_{CM_i}$  are private key of  $CM_{ij}$ . Therefore, the adversary cannot impersonate  $CM_{ij}$  to Sink. To attack Sink to  $CM_{kl}$ , an adversary has to generate a data  $M_2 = \{AD_{CM_{ij}}, T_2, V_1, V_3, R_1^*, R_s^*\}$ , where  $V_3 = H_3(s_{1SRk}AD_s, s_{3SRk}AD_{CM_{kl}}, R_s^*, R_1^*, T_2, V_1)$ . Without the knowledge of  $s_{1SRk}AD_s$  and  $s_{3SRk}AD_{CM_{kl}}$ , an adversary cannot generate  $V_3$ . Thus, the adversary cannot impersonate Sink to  $CM_{kl}$ . To impersonate  $CM_{kl}$  to  $CM_{ij}$ , an adversary has to generate a legal message  $M_3 = \{AD_{CM_{kl}}, T_3, V_4\}$ . Here the authentication value  $V_4 = H_2(k^*, AD_{CM_{kl}}, AD_{CM_{ij}}, T_3)$ . The adversary cannot compute  $V_4$  since he/she does not know the temporary key  $k^*$ . Therefore, the adversary cannot impersonate  $CM_{ij}$  to  $CM_{kl}$ .

### 6.3. Security Comparison

We compared the proposed scheme with Lee and Kim's scheme and Guo *et al.*'s scheme in terms of security properties. Similar to the Kim's work, P1, P2, P3, P4, P5 and P6 denote the key agreement, the authentication, the impersonation attack, the key freshness, the replay attack and the insider attack, separately. According to Table 2, we can conclude that the proposed scheme delivers a higher level of security compared to related works.

**Table 2. The Security Comparison**

	Ours	Lee and Kim's [7]	Kim's[24]	Guo <i>et al.</i> 's [8]
P1	Provide	Provide	Provide	Provide
P2	Provide	Provide	Provide	Provide
P3	Resistance	Resistance	Resistance	Resistance
P4	Resistance	Provide	N/A	N/A
P5	Resistance	N/A	N/A	N/A
P6	Resistance	N/A	N/A	N/A

## 7. Conclusion

We discuss several security weaknesses in the paper under a new security model. There is an adversary who can legally get the private parameter of CM or CH and control the channel between two CMs in the attack model. After that, we point out the two weaknesses of Lee and Kim's scheme [7] in our model. Then we propose an enhanced scheme based on the bilinear pair to overcome these weaknesses. Our proposal increases its security strength by using the Sink nodes. The forthcoming work is to achieve a formal proof method of the key agreement scheme in WSN. Then we achieve it in the real sensor hardware environments.

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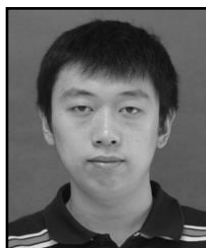
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