

EMD Based Curve Evolution Method for Segmentation of Lungs on CT Scan Images

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Abstract

Medical imaging is the technique that is used to produce images of the human body or parts for clinical purpose. The CT image provides thorough information of structure of lungs, which could be used for better surgical preparation for treating Lung Cancer features. This work proposes a method for segmentation of lungs from the given CT images. Here a curve evolutionary framework for segmentation is used. The flow fields driving the curves are based on the distributions of features in the inner and outer regions bounded by the curves. The segmentation method is automatic and shows good result.

Index terms: histogram, lung lobes, EMD, CT images

1. Introduction

Computer Tomography (CT) is one of the most efficient medical diagnostic methods and has currently a widespread usage. Multi-slice CT scanning technology has revolutionized screening of the lungs and inspires necessitate for pulmonary image analysis. Segmentation of the lungs and lobes is a prerequisite for such image analysis in chest CT scans. CT scan is more appropriate for showing the detailed information of the parts of human body and it is used for various applications such as detection, classification etc. The analysis of lungs in CT image is used to detect the airway and the vessel present in the lungs [6]. The human lungs are subdivided into distinct pulmonary lobes separated by thin barriers, called fissures. Each lobe contains separate supply branches for both vessels and airways. The segmentation of anatomical parts is important in the detection of pathological abnormalities present in the lungs. Segmentation of the pulmonary lobes is relevant in many clinical applications. Accurate lung segmentation allows for the detection and quantification of abnormalities within the lungs. The lobes are separately supplied by the first subdivisions of the bronchial tree after the main bronchi. The lobes function independently within the lungs. Segmentation of the pulmonary lobes is relevant in clinical practice and particularly challenging for cases with severe diseases or incomplete fissures. Pulmonary fissure is a boundary between the lobes in the lungs. Its segmentation is of clinical interest as it facilitates the assessment of lung disease on a lobar level. A new approach has been made for segmenting the major fissures in both lungs on thin-section computed tomography (CT) [5]. An image transformation called “ridge map” is proposed for enhancing the appearance of fissures on CT. A curve-growing process, modeled by a Bayesian network, is described that is influenced by both the features of the ridge map and prior knowledge of the shape of the fissure. The process is implemented in an adaptive regularization framework that balances these influences and reflects the causal dependencies in the Bayesian network using an entropy measure. This method effectively alleviates the problem of inappropriate weights of

regularization terms, an effect that can occur with static regularization methods. The method was applied to segment and visualize the lobes of the lungs on chest CT of 10 patients with pulmonary nodules. Only 78 out of 3286 left or right lung regions with fissures (2.4%) required manual correction. The average distance between the automatically segmented and the manually delineated ground truth fissures was 1.01 mm, which was similar to the average distance of 1.03 mm between two sets of manually segmented fissures. The method has a linear-time worst-case complexity and segments the upper lung from the lower lung on a standard computer is less than 5 minutes. The general problem of histogram based curve evolution is considered. The novel flow fields derived to guide the evolution process are based on using the Earth Mover's Distance for measuring the dissimilarity between two histograms.

1.1. Histogram-Based Methods

Histogram-based methods [4] are very efficient when compared to other image segmentation methods because they typically require only one pass through the pixels. In this technique, a histogram is computed from all of the pixels in the image, and the peaks and valleys in the histogram are used to locate the clusters in the image. Color or intensity can be used as the measure.

A refinement of this technique is to recursively apply the histogram-seeking method to cluster in the image in order to divide them into smaller clusters. This is repeated with smaller and smaller clusters until no more clusters are formed.

One disadvantage of the histogram-seeking method is that it may be difficult to identify significant peaks and valleys in the image. In this technique of image classification, distance metric and integrated region matching are familiar.

Histogram-based approaches can also be quickly adapted to occur over multiple frames, while maintaining their single pass efficiency. The histogram can be done in multiple fashions when multiple frames are considered. The same approach that is taken with one frame can be applied to multiple, and after the results are merged, peaks and valleys that were previously difficult to identify are more likely to be distinguishable. The histogram can also be applied on a per pixel basis where the information results are used to determine the most frequent color for the pixel location. This approach segments based on active objects and a static environment, resulting in a different type of segmentation is useful in video tracking.

1.2. Edge Detection

Edge Detection is a well-developed field on its own within image processing. Region boundaries and edges are closely related. Since there is often a sharp adjustment in intensity at the region boundaries, Edge detection techniques have therefore been used as the base of another segmentation technique.

The edges identified by edge detection are often disconnected. To segment an object from an image, however, one needs closed region boundaries. Edge is nothing but boundary between two images. Edge detection techniques refer to the identifying and locating the sharp discontinuities in the images.

The shape of an object can be either in terms of its boundary or in terms of the region it occupies. The shape representation based on boundary information requires image edge detection in this approach.

2. Methodology

2.1. Lung Segmentation using EMD

Image segmentation is a process of portioning an image into non overlapped, consistent regions that are homogeneous with respect to some characteristics like intensity, color, tone or texture and more [3]. Here a curve evolutionary framework for segmentation is used. The flow fields driving the curves are based on the distributions of features in the inner and outer regions bounded by the curves. So the general problem of histogram-based curve evolution is considered by deriving the novel fields to guide the evolution process based on using the Earth Mover's Distance (EMD) [2] for measuring the dissimilarity between the two histograms.

Active contours [9, 1, 8, 7] techniques were originally based on flow fields derived by integrating region boundary image data such as edge strength. The descriptors integrated within a region may also depend on the region. First there is a need to derive the gradient flow fields with respect to the Earth Mover's Distance metric.

The EMD

Let $P = \{p_1, \dots, p_N\}$ and $Q = \{q_1, \dots, q_N\}$ be the discrete probability distribution on N bins. Let $\{P_1, \dots, P_N=1\}$ and $\{Q_1, \dots, Q_N=1\}$ be the corresponding cumulative distribution functions(CDF). Then

$$EMD(P, Q) = \sum_{i=1}^N |P_i - Q_i| \quad (1)$$

Initialization

1. Initialize two cluster centers C_1 and C_2 by choosing randomly from $\{Q_1, \dots, Q_M\}$
2. For each Q_i compare $EMD(Q_i, C_1)$ and $EMD(Q_i, C_2)$. Assign Q_i to closer cluster centre.
3. Update C_1, C_2 by summing the counts of all assigned Q_i s:
- 4.

$$C_j^{new} = \sum_{\{i | label(i)=j\}} Q_i \quad (2)$$

2.2 Curve Evolution Based on EMD

Maximal-Discrepancy Functional

Let Ω be a closed curve in a image plane.

Let $CDF_R(Z_i) = \text{Prob}(\text{feature value in region } R \leq Z_i)$ (3)

Where $R = \{\text{in, out}\}$ separated by Ω

To measure the discrepancy by EMD

$$\begin{aligned} EMD(\Omega) &= EMD(P_{in}, P_{out}) \\ &= \sum_{i=1}^N |CDF_{in}(z_i) - CDF_{out}(z_i)| \end{aligned} \quad (4)$$

To represent the function (4) as a sum of (absolute value of) expressions of the form

$$\int \int_{\Omega_{out}} k_{z_i}^{out}(x, y, \Omega_{out}) dx dy + \int \int_{\Omega_{in}} k_{z_i}^{in}(x, y, \Omega_{in}) dx dy \quad (5)$$

Let us define $V(z_i, \Omega) = CDF_{in}(z_i) - CDF_{out}(z_i)$ and

$$T_z(x, y) = \begin{cases} 1, & I(x, y) \leq z \\ 0, & I(x, y) > z, \end{cases} \quad (6)$$

Where $I(x, y)$ is the feature value at (x, y) . Then,

$$CDF_R(z_i) = Prob(I(x, y) \leq z_i | (x, y) \in R) = \frac{\int \int_R T_{z_i}(x, y) dx dy}{\int \int_R 1 dx dy} \quad (7)$$

Denote the denominator by

$$A_R = G_1^R = \int \int_R 1 dx dy \text{ and define}$$

$$k_{z_i}^{in}(x, y, \Omega) = g^{in}(x, y, G_1^{in}) = \frac{T_{z_i}(x, y)}{G_1^{in}}$$

Then,

$$CDF_{in}(z_i) = \int \int_{\Omega_{in}} k_{z_i}^{in}(x, y, \Omega) dx dy = \int \int_{\Omega_{in}} \frac{T_{z_i}(x, y)}{G_1^{in}} dx dy.$$

and in a similar fashion,

$$-CDF_{out}(z_i) = \int \int_{\Omega_{out}} k_{z_i}^{out}(x, y, \Omega) dx dy = \int \int_{\Omega_{out}} -\frac{T_{z_i}(x, y)}{G_1^{in}} dx dy.$$

the flow that minimizes

$$V(z_i, \Omega) = \int \int_{\Omega_{out}} k_{z_i}^{out}(x, y, \Omega_{out}) dx dy + \int \int_{\Omega_{in}} k_{z_i}^{in}(x, y, \Omega_{in}) dx dy$$

is given by

$$\vec{F} = [k_{z_i}^{in} - k_{z_i}^{out} + A_1^{in} H_1^{in} - A_1^{out} H_1^{out}] \vec{N}, \quad (8)$$

Where \vec{N} is the inward normal to the curve, and $A_1^{out} H_1^{out}$ are as follows:

$$\begin{aligned} A_1^{in} &= \int \int_{\Omega_{in}} \frac{\partial g^{in}}{\partial G_1^{in}}(x, y, G_1^{in}) dx dy = \int \int_{\Omega_{in}} \frac{-T_{z_i}(x, y)}{G_1^{in^2}} dx dy \\ &= -\frac{1}{G_1^{in^2}} \int \int_{\Omega_{in}} T_{z_i}(x, y) dx dy \end{aligned} \quad (9)$$

And $H_1^{in} = 1$ (G_1^{in} integrates 1 over Ω_{in}). Similarly, $A_1^{out} = \frac{1}{G_1^{in^2}} \int \int_{\Omega_{out}} T_{z_i}(x, y) dx dy$.

Plugging everything in (8), and writing A_{in} , A_{out} instead of G_1^{in} , G_1^{out} , we obtain

$$\vec{F}_{z_i}(x, y) = \left[\frac{T_{z_i}(x,y)}{A_{in}} + \frac{T_{z_i}(x,y)}{A_{out}} - \frac{C_{in}}{A_{in}^2} - \frac{C_{out}}{A_{out}^2} \right] \vec{N}. \quad (10)$$

$$C_{in} = \iint_{\Omega_{in}} T_{z_i}(x, y) dx dy \quad (11)$$

=Number of pixels inside, where $I(x, y) \leq z_i$.

$$C_{out} = \iint_{out} T_{z_i}(x, y) dx dy \quad (12)$$

=Number of pixels outside, where $I(x, y) \leq z_i$

This flow minimizes $N(z_i, \Omega) = CDF_{in}(z_i) = CDF_{out}(z_i)$, since we want to maximize

$$EMD(\Omega) = \sum_{i=1}^N |CDF_{in}(z_i) - CDF_{out}(z_i)|,$$

The resulting flow is computed as follows:

Algorithm 1.

1. For every threshold z_i , compute

$$s_i = \text{sign}|CDF_{in}(z_i) - CDF_{out}(z_i)| = \begin{cases} 1, & CDF_{in}(z_i) \geq CDF_{out}(z_i) \\ -1, & CDF_{in}(z_i) \leq CDF_{out}(z_i) \end{cases} \quad (13)$$

3. Compute

$$F_{z_i}(x, y) = \left[T_{z_i}(x, y) \left(\frac{1}{A_{in}} + \frac{1}{A_{out}} \right) - \frac{C_{in}}{A_{in}^2} - \frac{C_{out}}{A_{out}^2} \right] \quad (14)$$

Where C_{in} , C_{out} and A_{in} , A_{out} are the areas of the inside and outside regions determined by Ω , respectively.

5. The overall flow field is then given by

$$T(x, y) = \sum_{z_i} (-s_i F_{z_i}(x, y)) \vec{N} \quad (15)$$

Where \vec{N} is the inward normal.

Match to template Functional

Another useful criterion is to measure how close the distribution inside the curve is to a given template distribution. Let H be the template histogram which is fixed and independent of the curve Ω . Let $J(\Omega) = EMD(\text{distribution inside } \Omega, H)$ be the functional then

$$J(\Omega) = \sum_{i=1}^N |CDF_{in}(z_i) - CDF_H(z_i)|. \quad (16)$$

Algorithm 2.

1. For every threshold z_i , compute $\alpha_i = CDF_H(z_i)$ and $s_i = sign|CDF_{in}(z_i) - \alpha_i|$.

2. Compute

$$F_{z_i}(x, y) = \left[T_{z_i}(x, y) \frac{1}{A_{in}} - \frac{C_{in}}{A_{in}^2} \right]. \quad (17)$$

Where C_{in} is as defined in (11) and A_{in} is the area of the inside region determined by Ω .

4. The overall flow field is

$$T(x, y) = \sum_{z_i} (s_i F_{z_i}(x, y)) \vec{N}, \quad (18)$$

Where \vec{N} is the inward normal.

Balloon Type Flow

To choose a more robust alternative by considering a normal flow where the speed is governed by a histogram difference metric. At each point (x, y) on the curve, a local histogram $Hist(x, y)$ of feature value is extracted. If H is the template histogram then flow at (x, y) is

$$\vec{F}(x, y) = -e^{-\alpha EMDh(Hist(x, y), H)} \vec{N} \quad (19)$$

3. Experimental Results

This algorithm is applied for any kind of gray level lung images. This algorithm is implemented in MATLAB software. The experiment results in segmenting the right and left lungs. This method finds the lungs by detecting the edges. In the final segmented image it can be specified by detecting its edges. It also uses refinement process to detect the edge.

The original image is shown in Figure 3.1(a). This is given as input. The following list of Figures 3.1(b,c,d,e) show the experimental results obtained by implementing Earth Mover’s Distance (EMD) on given CT lung images. Figure 3.1(f) shows the final segmented image. The experimental results show good accuracy.



Figure 3.1. (a) Original Input Image Figure 3.1. (b) Segmented Image Initial Stage

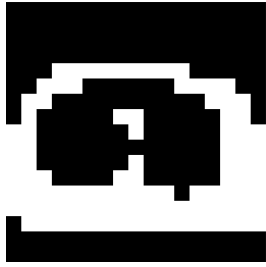


Figure 3.1. (c) Maximum Discrepancy Function

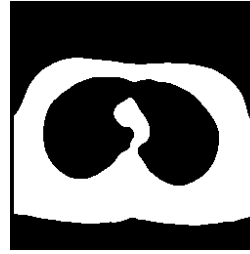


Figure 3.1. (d) Partial Refinement Image

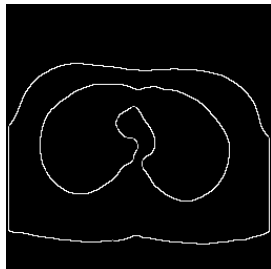


Figure 3.1. (e) Edge Image Refinement Process



Figure 3.1. (f) Final Segmental Image

4. Performance Evaluation

The different CT images are considered as input images as shown in Figure 4.1. The steps for the proposed work are performed for each input image and a final lung segmented image is obtained. This output lung segment image is compared with the accurate lung segment image. Then the accuracy is determined for each input image by comparing the count of pixel values with the accurate lung image. The following Table 4.1 gives the accuracy.

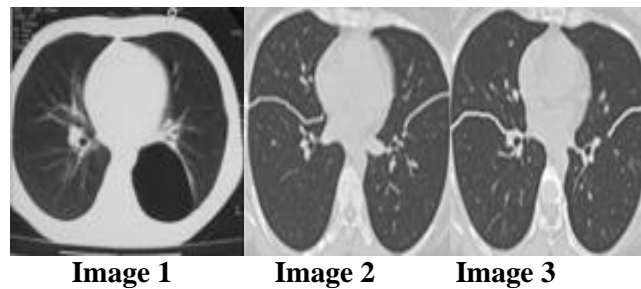


Figure 4.1. Original Images

Table 4.1. Accuracy of Lobe Segmentation for Various CT Images

Images	Accuracy
1	99.46 %
2	99.27 %
3	98.07 %

5. Conclusion

Segmentation of Lung lobes and fissures for surgical planning of treatment of Lung Cancer is proposed in this method. Lung is segmented from chest CT scan images using EMD Based technique. Further processing is carried out to visualize fissure characteristics and each segment inside the lung. Lung fissures are extracted using canny edge detection. The main modules of this work are Preprocessing, Lung Segmentation by EMD Base method and fissure Extraction. Lobe segmentation is carried out by edge tracking and region filling algorithms to differentiate the segments. The segmentation method is automatic and shows good accuracy. The future work concentrates on lobe segmentation to make the accurate result. In this paper, a novel edge detection approach is described. A number of experiments were conducted and the results show that the designed EMD based method.

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